

# Electronic State Structure and Optical Properties of $\text{Tb}(\text{oda})_3^{3-}$ Complexes in Trigonal $\text{Na}_3[\text{Tb}(\text{oda})_3] \cdot 2\text{NaClO}_4 \cdot 6\text{H}_2\text{O}$ Crystals<sup>†</sup>

Todd A. Hopkins, David H. Metcalf, and F. S. Richardson\*

Department of Chemistry, University of Virginia, Charlottesville, Virginia 22901

Received August 29, 1997

Polarized optical absorption and emission measurements are used to locate and assign 95 crystal-field energy levels split out of the  $4f^8$  electronic configuration of  $\text{Tb}^{3+}$  in single crystals of  $\text{Na}_3[\text{Tb}(\text{oda})_3] \cdot 2\text{NaClO}_4 \cdot 6\text{H}_2\text{O}$  (where oda denotes an oxydiacetate ligand). The absorption measurements span the 235–490 nm wavelength range, and the emission measurements span the 485–685 nm wavelength range. The combined absorption and emission spectra measurements provide access to the energy-level structures of 46 different  $4f^8[\text{SL}]J$  multiplet manifolds of  $\text{Tb}^{3+}$  (all multiplet manifolds with baricenter energies  $<42\,400\text{ cm}^{-1}$  above ground). The site symmetry of the  $\text{Tb}^{3+}$  ions in  $\text{Na}_3[\text{Tb}(\text{oda})_3] \cdot 2\text{NaClO}_4 \cdot 6\text{H}_2\text{O}$  is  $D_3$ , and the point-group symmetry of the tris-tetrate  $\text{Tb}(\text{oda})_3^{3-}$  coordination complexes is also  $D_3$ . The  $\text{Tb}(\text{oda})_3^{3-}$  complexes are chiral, and they exist in just one, fully resolved enantiomeric form in single crystals of  $\text{Na}_3[\text{Tb}(\text{oda})_3] \cdot 2\text{NaClO}_4 \cdot 6\text{H}_2\text{O}$ . The crystals exhibit strong chiroptical activity in their absorption and emission spectra, and results obtained from both circularly polarized and linearly polarized optical spectra measurements are used in making transition line assignments. The energy-level data acquired from the spectroscopic measurements are analyzed in terms of a model Hamiltonian that includes consideration of both isotropic and nonisotropic  $4f$  electron/crystal-field interactions, and the interaction parameters derived from this analysis are discussed and then compared with those obtained for other  $\text{Na}_3[\text{Ln}(\text{oda})_3] \cdot 2\text{NaClO}_4 \cdot 6\text{H}_2\text{O}$  systems and for  $\text{Tb}^{3+}$  in other crystalline hosts.

## Introduction

The tris-terdentate coordination complexes formed by the chelation of three oxydiacetate (oda) ligands to a trivalent lanthanide ion ( $\text{Ln}^{3+}$ ) have been studied extensively to elicit information about the effects of ligand structural complexity on the details of  $\text{Ln}^{3+}(4f^N)$  electronic state structure and optical properties. In these complexes, denoted here by  $\text{Ln}(\text{oda})_3^{3-}$ , each oda ligand is coordinated to the lanthanide ion via two negatively charged oxygen atoms (one from each of the two carboxylate moieties in oda) and a neutral ether oxygen atom. The  $\text{LnO}_9$  coordination cluster in these complexes forms a slightly distorted tri-capped trigonal-prism polyhedron of trigonal-dihedral ( $D_3$ ) symmetry, with the top and bottom triangles of this polyhedron defined by carboxylate oxygen donor atoms and the capping positions (on normals to the rectangular faces) occupied by ether oxygen atoms. The backbone of each bicyclic  $\text{Ln}(\text{oda})$  chelate ring system is nearly planar and stretches diagonally across a rectangular face of the  $\text{LnO}_9$  trigonal-prism structure. The chelate rings contain highly anisotropic charge distributions, and their interactions with the lanthanide  $4f$  electrons produce effects not ordinarily observed in structurally simpler systems.

The equilibrium structures of  $\text{Ln}(\text{oda})_3^{3-}$  complexes have trigonal-dihedral ( $D_3$ ) symmetry, and in aqueous solution these complexes exist as a racemic mixture of rapidly interconverting optical isomers (enantiomers) which are often denoted as  $\Lambda$ - $\text{Ln}(\text{oda})_3^{3-}$  and  $\Delta$ - $\text{Ln}(\text{oda})_3^{3-}$ . However, in single crystals of  $\text{Na}_3[\text{Ln}(\text{oda})_3] \cdot 2\text{NaClO}_4 \cdot 6\text{H}_2\text{O}$  grown from aqueous solution, all of the  $\text{Ln}(\text{oda})_3^{3-}$  complexes are of like enantiomeric form (either  $\Lambda$  or  $\Delta$ ), and these crystals exhibit chiroptical properties that

have proved to be useful in characterizing the electronic energy-level structures and optical transition mechanisms in  $\text{Ln}(\text{oda})_3^{3-}$  complexes.<sup>1,2</sup> At room temperature, these crystals have trigonal,  $R32$  space-group symmetry, with three  $\text{Ln}(\text{oda})_3^{3-}$  complexes per unit cell and with the  $\text{Ln}^{3+}$  ions located at sites of  $D_3$  point-group symmetry.<sup>3–6</sup> The macroscopic uniaxial symmetry of these crystals is generally maintained over extended temperature ranges below 300 K, though for several members of the lanthanide series there is spectroscopic evidence that the  $\text{Ln}^{3+}$  site symmetry is lower than  $D_3$  at temperatures below 120 K.<sup>2</sup> Optical-quality single crystals of  $\text{Na}_3[\text{Ln}(\text{oda})_3] \cdot 2\text{NaClO}_4 \cdot 6\text{H}_2\text{O}$  compounds are relatively easy to grow, and they have been used extensively in detailed studies of electronic state structure and optical processes in  $\text{Ln}(\text{oda})_3^{3-}$  complexes. Among these complexes, the most thoroughly studied have been those of neodymium ( $\text{Nd}^{3+}$ ),<sup>7–11</sup> samarium ( $\text{Sm}^{3+}$ ),<sup>12–15</sup> europium ( $\text{Eu}^{3+}$ ),<sup>16–19</sup> gadolinium ( $\text{Gd}^{3+}$ ),<sup>20–23</sup> dysprosium ( $\text{Dy}^{3+}$ ),<sup>24</sup>

- (1) Richardson, F. S.; Faulkner, T. R. *J. Chem. Phys.* **1982**, *76*, 1595.
- (2) Richardson, F. S. *J. Less-Common Met.* **1989**, *149*, 161.
- (3) Albertsson, J. *Acta Chem. Scand.* **1968**, *22*, 1563.
- (4) Albertsson, J. *Acta Chem. Scand.* **1970**, *24*, 3527.
- (5) Albertsson, J.; Elding, I. *Acta Chem. Scand., Ser. A* **1977**, *31*, 21.
- (6) Fronczek, F. R.; Banerjee, A. K.; Watkins, S. F.; Schwartz, R. W. *Inorg. Chem.* **1981**, *20*, 2745.
- (7) Vala, M.; Szczepanski, J.; Banerjee, A. K.; Chowdhury, M. *Chem. Phys.* **1989**, *134*, 149.
- (8) May, P. S.; Jayasankar, C. K.; Richardson, F. S. *Chem. Phys.* **1989**, *138*, 123.
- (9) May, P. S.; Jayasankar, C. K.; Richardson, F. S. *Chem. Phys.* **1989**, *138*, 139.
- (10) May, P. S. Ph.D. Dissertation, University of Virginia, 1988.
- (11) Fluyt, L.; Couwenberg, I.; Lambaerts, H.; Binnemans, K.; Görlner-Walrand, C.; Reid, M. F. *J. Chem. Phys.* **1996**, *105*, 6117.
- (12) May, P. S.; Reid, M. F.; Richardson, F. S. *Mol. Phys.* **1987**, *61*, 1455.
- (13) May, P. S.; Reid, M. F.; Richardson, F. S. *Mol. Phys.* **1987**, *61*, 1471.
- (14) May, P. S.; Reid, M. F.; Richardson, F. S. *Mol. Phys.* **1987**, *62*, 341.

\* To whom correspondence should be addressed.

<sup>†</sup> "oda" is oxydiacetate ( $-\text{OOCCH}_2\text{OCH}_2\text{COO}^-$ ).

holmium ( $\text{Ho}^{3+}$ ),<sup>25–27</sup> and erbium ( $\text{Er}^{3+}$ ),<sup>28,29</sup> Optical studies of the praseodymium ( $\text{Pr}^{3+}$ ),<sup>30</sup> terbium ( $\text{Tb}^{3+}$ ),<sup>31</sup> and thulium ( $\text{Tm}^{3+}$ )<sup>32</sup> complexes have also been reported, but without detailed analyses of energy-level structure.

In the present paper, we report the first detailed analysis of  $4f^8(\text{Tb}^{3+})$  electronic energy-level structure in  $\text{Tb}(\text{oda})_3^{3-}$  complexes, using data obtained from optical (and chiroptical) absorption and emission measurements performed on single crystals of  $\text{Na}_3[\text{Ln}(\text{oda})_3] \cdot 2\text{NaClO}_4 \cdot 6\text{H}_2\text{O}$ , which we shall denote hereafter as TbODA. The  $4f^8$  electronic energy-level structure of  $\text{Tb}^{3+}$  in TbODA presented a somewhat more difficult challenge for measurement and analysis than was encountered in our previous work on other  $\text{Ln}(\text{oda})_3^{3-}$  (and LnODA) systems, but eventually the combined measurement and analysis techniques permitted the location and symmetry assignment of 95 (of the 314 total) crystal-field levels split out of the 46 lowest-energy  $4f^8[\text{SL}]J$  multiplet manifolds of  $\text{Tb}^{3+}$  in TbODA. These levels span the 0–42 400  $\text{cm}^{-1}$  energy range (above ground), and they provided an adequate basis for performing parametric modeling calculations of crystal-field interaction strengths in TbODA. The parametrized model Hamiltonian derived from these calculations produced an eigenvalue spectrum in which the rms deviation between calculated and observed energy levels is  $<12 \text{ cm}^{-1}$ . The overall crystal-field interaction strength determined for  $\text{Tb}^{3+}(4f^8)$  in TbODA is found to be somewhat greater than that determined for  $\text{Tb}^{3+}(4f^8)$  in single crystals of  $\text{Na}_3[\text{Yb}_{0.95}\text{Tb}_{0.05}(\text{dpa})_3] \cdot \text{NaClO}_4 \cdot 10\text{H}_2\text{O}$ , where in the latter the  $\text{Tb}^{3+}$  ions are each coordinated to three dipicolinate (dpa) ligands via tris-terdentate chelation.<sup>33</sup> The overall crystal-field interaction strength determined for TbODA is also greater than those determined for any of the other LnODA systems that have been studied so far.

The experimental work performed in the study reported here included measurements of unpolarized, circularly polarized, and  $\sigma$  and  $\pi$  linearly polarized optical absorption and emission spectra, under variable sample-temperature conditions. The absorption spectra measurements spanned the 235–490 nm wavelength range, and the emission spectra measurements spanned the 485–685 nm wavelength range. All of the

luminescence observed for TbODA originates from the lowest  $^5\text{D}_4$  multiplet manifold of  $\text{Tb}^{3+}(4f^8)$ , which is centered at ca. 20 480  $\text{cm}^{-1}$  above ground. The emission spectra recorded for TbODA encompass all transitions that originate from this  $^5\text{D}_4$  multiplet manifold and terminate on levels split out of the seven  $^7\text{F}_J$  ( $J = 0–6$ ) multiplet manifolds derived from the  $^7\text{F}$  (*ground*) term of the  $4f^8(\text{Tb}^{3+})$  electronic configuration. The lowest-energy (*ground*) multiplet of  $4f^8(\text{Tb}^{3+})$  is  $^7\text{F}_6$ , and all transitions observed in the recorded absorption spectra originate from crystal-field (Stark) levels split out of this multiplet manifold. In a crystal field of trigonal-dihedral ( $D_3$ ) symmetry, the  $^7\text{F}_6$  multiplet is split into nine Stark levels, four of which are doubly degenerate. In TbODA, the total splitting between the lowest- and highest-energy Stark levels of  $^7\text{F}_6$  is only about 200  $\text{cm}^{-1}$ , so under room-temperature conditions all nine of the Stark levels split out of  $^7\text{F}_6$  are thermally accessible.

## Experimental Methods

**Compound and Crystal Sample Preparation.** Single crystals of  $\text{Na}_3[\text{Tb}(\text{oda})_3] \cdot 2\text{NaClO}_4 \cdot 6\text{H}_2\text{O}$  were grown according to the methods of Albertsson.<sup>3,4</sup> Crystals harvested for optical measurements were typically ca. 1–2 mm thick. The crystal samples were attached to copper mounts built for use in the cold head of an optical cryostat. To ensure proper thermal contact, the crystals were mounted using Crycon grease and indium foil at cold-head–crystal interfaces. The crystals were mounted in orientations defined with respect to the alignment of their unique axis relative to the direction of light propagation in the optical absorption experiments and the direction of excitation and emission detection in the optical emission experiments. Parallel alignment of the unique axis and the direction of light propagation is referred to here as an *axial* orientation. Perpendicular alignment of the unique axis and the direction of light propagation is referred to here as an *orthoaxial* orientation.

In our initial optical experiments, the crystal samples were lightly coated with Crycon grease to inhibit their possible deterioration (via efflorescence) under the high-vacuum conditions in the closed-cycle helium refrigerator/cryostat. However, a repeat of these experiments with unprotected crystal samples yielded essentially identical results, and the crystals showed no signs of deterioration during multiple up-and-down temperature changes (between ca. 10 and 293 K) in the cryostat.

**Optical Absorption Measurements.** Circularly polarized and unpolarized *axial*, and  $\sigma$  and  $\pi$  linearly polarized *orthoaxial* spectra were measured for TbODA. All of the unpolarized axial, and  $\sigma$  and  $\pi$  polarized *orthoaxial* absorption spectra were obtained with a Cary Model 5 UV–VIS–NIR spectrophotometer. A CTI-cryogenic pump closed-cycle helium refrigerator model 22C controlled by a Lake Shore cryotronics temperature-controller (model DRC-70) was used to achieve cold-head temperatures of either 70 or 20 K. Absorption spectra were recorded over the 235–490 nm wavelength range. The *orthoaxial* spectral measurements were taken by fitting a linear polarizing element into the spectrophotometer.

Circular dichroism (CD) spectra were measured using instrumentation constructed in our laboratory at the University of Virginia. Broad-band radiation from a xenon arc lamp (500 W, PTI A5000 housing) was used as the excitation source. The excitation light was passed through a linear-polarizing element followed by a Hinds International PEM-80 photoelastic modulator. The polarizer–PEM combination polarizes the excitation light into left and right circularly polarized components. The PEM served as a dynamic polarizer, operating at a modulation frequency of ca. 50 kHz, that alternately transmitted left and right circularly polarized light which was then passed through the sample crystal. The transmitted light was dispersed with a 0.75 m double-grating monochromator, and the transmission intensity was measured using photon-counting techniques. The transmission spectrum was converted to a CD spectrum by correcting for the arc-lamp output profile.

**Optical Emission Measurements.** Optical emission spectra were measured using instrumentation constructed in our laboratory at the

- (15) May, P. S.; Metcalf, D. H.; Richardson, F. S.; Carter, R. C.; Miller, C. E.; Palmer, R. A. *J. Lumin.* **1992**, *51*, 249.
- (16) Berry, M. T.; Schwieters, C.; Richardson, F. S. *Chem. Phys.* **1988**, *122*, 105.
- (17) Berry, M. T.; Schwieters, C.; Richardson, F. S. *Chem. Phys.* **1988**, *122*, 125.
- (18) May, P. S.; Richardson, F. S. *Chem. Phys. Lett.* **1991**, *179*, 277.
- (19) Görrler-Walrand, C.; Verhoeven, P.; D'Olieslager, J.; Fluyt, L.; Binne-mans, K. *J. Chem. Phys.* **1994**, *100*, 815.
- (20) Kundu, T.; Banerjee, A. K.; Chowdhury, M. *Phys. Rev. B* **1990**, *41*, 10911.
- (21) Stephens, E. M.; Metcalf, D. H.; Berry, M. T.; Richardson, F. S. *Phys. Rev. B* **1991**, *44*, 9895.
- (22) Kundu, T.; Banerjee, A. K.; Chowdhury, M. *Chem. Phys.* **1991**, *156*, 95.
- (23) Gunde, K. E.; Richardson, F. S. *Chem. Phys.* **1995**, *194*, 195.
- (24) Metcalf, D. H.; Hopkins, T. A.; Richardson, F. S. *Inorg. Chem.* **1995**, *34*, 4868.
- (25) Moran, D. M.; De Piante, A.; Richardson, F. S. *Phys. Rev. B* **1990**, *42*, 3317.
- (26) Moran, D. M.; Richardson, F. S. *Phys. Rev. B* **1990**, *42*, 3331.
- (27) Moran, D. M.; Richardson, F. S. *Inorg. Chem.* **1992**, *31*, 813.
- (28) Schoene, K. A.; Quagliano, J. R.; Richardson, F. S. *Inorg. Chem.* **1991**, *30*, 3803.
- (29) Schoene, K. A. Ph.D. Dissertation, University of Virginia, 1989.
- (30) Schwartz, R. W.; Banerjee, A. K.; Sen, A. C.; Chowdhury, M. *J. Chem. Soc., Faraday Trans. 2* **1980**, *76*, 620.
- (31) Saxe, J. D.; Morley, J. P.; Richardson, F. S. *Mol. Phys.* **1982**, *47*, 407.
- (32) Hammond, R. M. Ph.D. Dissertation, University of Virginia, 1988.
- (33) Hopkins, T. A.; Bolender, J. P.; Metcalf, D. H.; Richardson, F. S. *Inorg. Chem.* **1996**, *35*, 5356.

University of Virginia. An argon ion ( $\text{Ar}^+$ ) laser was used as an excitation source; sample luminescence was dispersed with a 0.75 m double-grating monochromator; and luminescence intensity was measured using photon-counting techniques. In all experiments, sample excitation was along the same direction as emission detection. Three different optical cryostats were used to control sample temperature in our emission experiments. A closed-cycle helium refrigerator was used in experiments carried out at 20 and 293 K, and a liquid nitrogen cooled cryostat was used in experiments carried out at 77 K. Single crystals of TbODA were mounted with their unique (optic) axis aligned either parallel or perpendicular to the direction of emission detection. Spectra obtained with the unique axis aligned parallel to the direction of emission detection are referred to as *axial* spectra, whereas those obtained with the unique axis aligned perpendicular to this direction are referred to as *orthoaxial* spectra.

For the trigonal TbODA crystals examined in this study, emission measured along the crystallographic *c* axis (i.e., unique axis), as in our axial measurements, can exhibit at least some degree of circular polarization, and emission measured along a direction that is *perpendicular* to the crystallographic *c* axis (as in our orthoaxial spectral measurements) can exhibit some degree of linear polarization. In our axial emission experiments, the sample luminescence was analyzed in terms of left and right circularly polarized intensity components, while in our orthoaxial emission experiments, the sample luminescence was analyzed in terms of intensity components polarized perpendicular ( $\sigma$ ) and parallel ( $\pi$ ) to the crystal *c* axis. This was done by using a PEM, operating at a modulation frequency of ca. 100 kHz, that alternately transmitted  $\sigma$  and  $\pi$  polarized luminescence intensities (for the orthoaxial measurements) to the emission detection unit of our spectrophotometer, and by using a PEM-polarizer (inverted order with respect to the CD measurements) combination that alternately transmitted left and right circularly polarized luminescence intensities to the emission detection unit of our spectrophotometer.

All of the luminescence intensity observed in our experiments originates from the  $^5\text{D}(3)_4$  excited multiplet of  $\text{Tb}^{3+}$  (centered at ca. 20 480  $\text{cm}^{-1}$  above ground). The energy gap between this multiplet and the next lower-energy multiplet ( $^7\text{F}_0$ ) is ca. 14700  $\text{cm}^{-1}$ , which is larger than any lattice phonon or molecular vibrational energy in TbODA crystals. Therefore, nonradiative decay processes for  $^5\text{D}(3)_4$  are relatively slow, and this multiplet exhibits a strong luminescence with a high quantum yield. The emission spectra measured in this study include all of the  $^7\text{F}_J$  ( $J = 0-6$ )  $\leftarrow$   $^5\text{D}(3)_4$  transition regions, spanning the 485–685 nm wavelength range. For the  $^7\text{F}_{0-5} \leftarrow ^5\text{D}(3)_4$  transition regions, the luminescence was excited with the 488.0 nm line of an argon ion laser, which corresponds to  $^7\text{F}_6 \leftarrow ^5\text{D}(3)_4$  excitation. The luminescence of the  $^7\text{F}_6 \leftarrow ^5\text{D}(3)_4$  transition region was excited with UV lines (in the 351–364 nm wavelength range) of an argon ion laser.

## Methods of Data Analysis

**Optical Selection Rules and Line Assignments.** The crystal-field energy levels split out of the  $4f^8$  electronic configuration of  $\text{Tb}^{3+}$  in TbODA may be classified as having  $A_1$ ,  $A_2$ , or E symmetry in the  $D_3$  point group, where  $A_1$ ,  $A_2$ , and E denote irreducible representation (irrep) labels in this group. Therefore, all transitions between crystal-field levels in TbODA may be classified (by symmetry) as  $A_1 \leftrightarrow A_1$ ,  $A_2 \leftrightarrow A_2$ ,  $A_1 \leftrightarrow A_2$ ,  $A_1 \leftrightarrow E$ ,  $A_2 \leftrightarrow E$ , or  $E \leftrightarrow E$ . The optical selection rules for each of these transition types depend on the polarization properties of the perturbing radiation and on the interactions responsible for the transitions. All transitions observed in the optical absorption and emission spectra measured in the present study may be presumed to occur via electric and/or magnetic dipole interaction mechanisms, and the relevant interaction operators for connecting crystal-field states are the electric dipole ( $\mu$ ) and magnetic dipole ( $m$ ) moment operators. Here we express these dipole operators in a spherical coordinate basis,  $q = 0, \pm 1$ , chosen such that for any given  $\text{Tb}(\text{oda})_3^{3-}$  complex in TbODA, the  $q = 0$  axis is defined to be coincident with the trigonal symmetry axis of the complex and, therefore, parallel to the unique (optic) axis of TbODA. Expressed in this basis, the  $\mu_0$  and  $m_0$  components of the  $\mu$  and  $m$  operators each transform as the  $A_2$  irrep

**Table 1.** Electric ( $\mu$ ) and Magnetic ( $m$ ) Dipole Selection Rules for Optical Absorption and Emission Measurements on  $\text{Tb}(\text{oda})_3^{3-}$  Complexes in Trigonal  $\text{Na}_3[\text{Tb}(\text{oda})_3] \cdot 2\text{NaClO}_4 \cdot 6\text{H}_2\text{O}$  Crystals

transition type <sup>a</sup>	axial spectra <sup>b</sup>	orthoaxial spectra <sup>c</sup>	
		$\sigma$ polarized	$\pi$ polarized
$A_1 \leftrightarrow A_1$	forbidden	forbidden	forbidden
$A_1 \leftrightarrow A_2$	forbidden	$m_0$	$\mu_0$
$A_2 \leftrightarrow A_2$	forbidden	forbidden	forbidden
$A_1 \leftrightarrow E$	$\mu_{\pm 1}; m_{\pm 1}$	$\mu_{\pm 1}$	$m_{\pm 1}$
$A_2 \leftrightarrow E$	$\mu_{\pm 1}; m_{\pm 1}$	$\mu_{\pm 1}$	$m_{\pm 1}$
$E \leftrightarrow E$	$\mu_{\pm 1}; m_{\pm 1}$	$\mu_{\pm 1}; m_0$	$\mu_0; m_{\pm 1}$

<sup>a</sup> Energy levels are labeled according to their irreducible representation (irrep) in the  $D_3$  point group. <sup>b</sup> Light propagating along the crystallographic *c* axis (the *unique* axis), which is parallel to the trigonal symmetry axes of the  $\text{Tb}(\text{oda})_3^{3-}$  complexes. <sup>c</sup> Light propagating along a direction perpendicular to the crystallographic *c* axis.

under the symmetry operations of the  $D_3$  point group, and the  $\mu_{\pm 1}$  and  $m_{\pm 1}$  components each transform as the E irrep under the symmetry operations of this group. Given these symmetry properties of the  $\mu_q$  and  $m_q$  operator components, electric and magnetic dipole selection rules are easily derived for each of the six transition types defined above. The selection rules relevant to the optical absorption and emission measurements performed on TbODA are shown in Table 1.

Nearly all of the transitions observed in the absorption spectra measured in this study are predicted, either by direct calculation or by application of  $\Delta J$ ,  $\Delta L$ , and  $\Delta S$  selection rules, to occur via predominantly *electric dipole* interaction mechanisms. Therefore, assignments of these transitions, with respect to symmetry type, could be made relatively unambiguously by applying the electric dipole selection rules of Table 1 to the combination of results obtained from our axial and polarized orthoaxial absorption intensity measurements. Similarly, the transitions observed in the  $^5\text{D}(3)_4 \rightarrow ^7\text{F}_6$ ,  $^7\text{F}_2$ ,  $^7\text{F}_1$ , and  $^7\text{F}_0$  emission regions of  $\text{Tb}^{3+}$  in TbODA are also expected to have predominantly electric dipole character and, therefore, be amenable to unambiguous symmetry assignment. However, the situation is somewhat different in the  $^5\text{D}(3)_4 \rightarrow ^7\text{F}_5$ ,  $^7\text{F}_4$ , and  $^7\text{F}_3$  emission regions, where many of the transitions are expected to exhibit line intensity and polarization properties that reflect both electric and magnetic dipole interaction mechanisms. Line assignments in these emission regions could not be based solely on applications of the selection rules given in Table 1, but they were aided by results obtained from *direct* calculations of magnetic dipole transition line strengths.

We note from Table 1 that the only transition types observable in our *axial* absorption and emission spectra measurements are those in which at least one of the connecting levels has E symmetry. These are the only transition types that appear in the circular dichroism (CD) and circularly polarized luminescence (CPL) spectra measured in this study.

**Energy Level Analysis.** The  $4f^8$  electronic energy-level structure of  $\text{Tb}^{3+}$  in TbODA was analyzed in terms of a model Hamiltonian that is fully commensurate with the model Hamiltonian employed previously in our studies of other LnODA systems.<sup>8,12,16,21,24,25,28</sup> It will be convenient for our discussions here to partition this Hamiltonian as follows:

$$\hat{H} = \hat{H}_a + \hat{H}_{\text{cf}}^+ \quad (1)$$

where  $\hat{H}_a$  is defined to incorporate the isotropic, *atomic-like* parts of  $\hat{H}$  (including the spherically symmetric parts of the  $4f$  electron/crystal-field interactions) and  $\hat{H}_{\text{cf}}^+$  is defined to represent the nonspherically symmetric components of the *even-parity* crystal field. We will refer to  $\hat{H}_a$  as the *atomic* Hamiltonian and will call  $\hat{H}_{\text{cf}}^+$  the *crystal-field* Hamiltonian. Both the  $\hat{H}_a$  and  $\hat{H}_{\text{cf}}^+$  parts of the model Hamiltonian are defined to operate entirely *within* the  $4f^8(\text{Tb}^{3+})$  electronic configuration; however,  $\hat{H}_a$  contains a number of “effective” two- and three-body interaction terms parametrized to include implicit consideration of interconfigurational mixings between  $4f^8$  and higher-energy configurations of like parity.

**Table 2.** Calculated and Experimentally Observed Crystal-field Energy Levels of Tb<sup>3+</sup> in Na<sub>3</sub>[Tb(oda)<sub>3</sub>]·2NaClO<sub>4</sub>·6H<sub>2</sub>O

level no.	term <sup>a</sup>	J <sup>a</sup>	Γ <sup>b</sup>	energy (cm <sup>-1</sup> )			level no.	term <sup>a</sup>	J <sup>a</sup>	Γ <sup>b</sup>	energy (cm <sup>-1</sup> )		
				calc <sup>c</sup>	expt <sup>d</sup>	Δ <sup>e</sup>					calc <sup>c</sup>	expt <sup>d</sup>	Δ <sup>e</sup>
1	<sup>7</sup> F	6	A <sub>1</sub>	-9	0	-9	68	<sup>5</sup> G (3)	5	E	27 741	27 741	0
2	<sup>7</sup> F	6	E	9	6	3	69	<sup>5</sup> G (3)	5	E	27 756	27 761	-5
3	<sup>7</sup> F	6	A <sub>2</sub>	21	18	3	70	<sup>5</sup> G (3)	5	A <sub>2</sub>	27 757	n.d.	
4	<sup>7</sup> F	6	A <sub>1</sub>	22	30	-8	71	<sup>5</sup> G (3)	5	A <sub>1</sub>	27 760	n.d.	
5	<sup>7</sup> F	6	E	50	68	-18	72	<sup>5</sup> G (3)	5	E	27 774	n.d.	
6	<sup>7</sup> F	6	A <sub>2</sub>	166	n.d.		73	<sup>5</sup> G (3)	5	E	27 823	27 832	-9
7	<sup>7</sup> F	6	E	172	n.d.		74	<sup>5</sup> G (3)	5	A <sub>2</sub>	27 851	n.d.	
8	<sup>7</sup> F	6	A <sub>1</sub>	176	n.d.		75	<sup>5</sup> D (3)	2	A <sub>1</sub>	28 121	n.d.	
9	<sup>7</sup> F	6	E	196	n.d.		76	<sup>5</sup> D (3)	2	E	28 141	28 139	2
10	<sup>7</sup> F	5	A <sub>1</sub>	2 013	2 047	-34	77	<sup>5</sup> D (3)	2	E	28 154	n.d.	
11	<sup>7</sup> F	5	A <sub>2</sub>	2 043	2 062	-19	78	<sup>5</sup> G (2)	4	A <sub>1</sub>	28 218	n.d.	
12	<sup>7</sup> F	5	E	2 061	2 078	-17	79	<sup>5</sup> G (2)	4	E	28 218	28 233	-15
13	<sup>7</sup> F	5	E	2 109	2 111	-2	80	<sup>5</sup> G (2)	4	A <sub>2</sub>	28 228	n.d.	
14	<sup>7</sup> F	5	E	2 148	2 146	2	81	<sup>5</sup> G (2)	4	A <sub>1</sub>	28 252	n.d.	
15	<sup>7</sup> F	5	E	2 257	n.d.		82	<sup>5</sup> G (2)	4	E	28 260	n.d.	
16	<sup>7</sup> F	5	A <sub>2</sub>	2 301	2 292	9	83	<sup>5</sup> G (2)	4	E	28 281	n.d.	
17	<sup>7</sup> F	4	A <sub>1</sub>	3 225	n.d.		84	<sup>5</sup> L	9	A <sub>2</sub>	28 315	n.d.	
18	<sup>7</sup> F	4	E	3 313	3 320	-7	85	<sup>5</sup> L	9	E	28 332	n.d.	
19	<sup>7</sup> F	4	A <sub>2</sub>	3 376	3 376	0	86	<sup>5</sup> L	9	E	28 373	n.d.	
20	<sup>7</sup> F	4	A <sub>1</sub>	3 415	3 398	17	87	<sup>5</sup> L	9	A <sub>1</sub>	28 388	n.d.	
21	<sup>7</sup> F	4	E	3 415	3 406	9	88	<sup>5</sup> L	9	E	28 425	n.d.	
22	<sup>7</sup> F	4	E	3 596	3 621	-25	89	<sup>5</sup> L	9	A <sub>2</sub>	28 454	n.d.	
23	<sup>7</sup> F	3	E	4 343	4 326	19	90	<sup>5</sup> L	9	A <sub>1</sub>	28 456	n.d.	
24	<sup>7</sup> F	3	A <sub>1</sub>	4 376	4 345	31	91	<sup>5</sup> L	9	E	28 465	28 478	-13
25	<sup>7</sup> F	3	E	4 401	4 405	-4	92	<sup>5</sup> L	9	E	28 517	n.d.	
26	<sup>7</sup> F	3	A <sub>2</sub>	4 408	4 414	-6	93	<sup>5</sup> L	9	A <sub>2</sub>	28 540	n.d.	
27	<sup>7</sup> F	3	A <sub>2</sub>	4 459	4 468	-9	94	<sup>5</sup> L	9	A <sub>1</sub>	28 549	n.d.	
28	<sup>7</sup> F	2	A <sub>1</sub>	5 015	4 992	23	95	<sup>5</sup> L	9	E	28 565	28 559	6
29	<sup>7</sup> F	2	E	5 056	5 055	1	96	<sup>5</sup> L	9	A <sub>2</sub>	28 587	28 609	-22
30	<sup>7</sup> F	2	E	5 159	5 157	2	97	<sup>5</sup> G (2)	3	A <sub>2</sub>	28 901	n.d.	
31	<sup>7</sup> F	1	A <sub>2</sub>	5 532	5 517	15	98	<sup>5</sup> G (2)	3	E	28 912	28 905	7
32	<sup>7</sup> F	1	E	5 540	5 534	6	99	<sup>5</sup> G (2)	3	A <sub>2</sub>	28 933	28 936	-3
33	<sup>7</sup> F	0	A <sub>1</sub>	5 756	5 750	6	100	<sup>5</sup> G (2)	3	A <sub>1</sub>	28 946	n.d.	
34	<sup>5</sup> D (3)	4	E	20 468	20 462	6	101	<sup>5</sup> G (2)	3	E	28 948	28 957	-9
35	<sup>5</sup> D (3)	4	A <sub>1</sub>	20 444	n.d.		102	<sup>5</sup> L	8	E	29 082	n.d.	
36	<sup>5</sup> D (3)	4	A <sub>2</sub>	20 467	20 468	-1	103	<sup>5</sup> L	8	A <sub>1</sub>	29 099	n.d.	
37	<sup>5</sup> D (3)	4	E	20 483	20 475	8	104	<sup>5</sup> L	8	E	29 108	29 106	2
38	<sup>5</sup> D (3)	4	A <sub>1</sub>	20 509	20 493	16	105	<sup>5</sup> L	8	A <sub>2</sub>	29 131	29 126	5
39	<sup>5</sup> D (3)	4	E	20 527	20 512	15	106	<sup>5</sup> L	8	A <sub>2</sub>	29 151	29 148	3
40	<sup>5</sup> D (3)	3	A <sub>2</sub>	26 143	26 147	-4	107	<sup>5</sup> L	8	A <sub>1</sub>	29 155	n.d.	
41	<sup>5</sup> D (3)	3	E	26 207	26 195	12	108	<sup>5</sup> L	8	E	29 173	29 179	-6
42	<sup>5</sup> D (3)	3	A <sub>1</sub>	26 213	n.d.		109	<sup>5</sup> L	8	E	29 200	n.d.	
43	<sup>5</sup> D (3)	3	E	26 234	26 219	15	110	<sup>5</sup> L	8	E	29 257	29 249	8
44	<sup>5</sup> D (3)	3	A <sub>2</sub>	26 246	26 265	-19	111	<sup>5</sup> L	8	E	29 271	n.d.	
45	<sup>5</sup> G (3)	6	A <sub>1</sub>	26 328	n.d.		112	<sup>5</sup> L	8	A <sub>1</sub>	29 290	n.d.	
46	<sup>5</sup> G (3)	6	E	26 386	26 381	5	113	<sup>5</sup> L	7	E	29 317	n.d.	
47	<sup>5</sup> G (3)	6	A <sub>2</sub>	26 416	n.d.		114	<sup>5</sup> G (2)	2	A <sub>1</sub>	29 347	n.d.	
48	<sup>5</sup> G (3)	6	A <sub>1</sub>	26 426	n.d.		115	<sup>5</sup> L	7	E	29 363	29 377	-14
49	<sup>5</sup> G (3)	6	E	26 434	26 429	5	116	<sup>5</sup> L	7	A <sub>2</sub>	29 378	n.d.	
50	<sup>5</sup> G (3)	6	A <sub>2</sub>	26 442	n.d.		117	<sup>5</sup> L	8	A <sub>1</sub>	29 403	n.d.	
51	<sup>5</sup> G (3)	6	E	26 459	n.d.		118	<sup>5</sup> G (2)	2	E	29 407	29 410	-3
52	<sup>5</sup> G (3)	6	A <sub>1</sub>	26 536	n.d.		119	<sup>5</sup> L	7	A <sub>2</sub>	29 419	n.d.	
53	<sup>5</sup> G (3)	6	E	26 552	26 535	17	120	<sup>5</sup> G (2)	2	E	29 447	n.d.	
54	<sup>5</sup> L	10	E	26 825	26 817	8	121	<sup>5</sup> L	7	E	29 471	29 464	7
55	<sup>5</sup> L	10	A <sub>2</sub>	26 825	n.d.		122	<sup>5</sup> L	7	E	29 503	n.d.	
56	<sup>5</sup> L	10	E	26 847	26 840	7	123	<sup>5</sup> L	7	A <sub>2</sub>	29 533	n.d.	
57	<sup>5</sup> L	10	A <sub>1</sub>	26 863	n.d.		124	<sup>5</sup> L	7	A <sub>1</sub>	29 570	n.d.	
58	<sup>5</sup> L	10	E	27 005	n.d.		125	<sup>5</sup> L	6	A <sub>1</sub>	29 590	n.d.	
59	<sup>5</sup> L	10	E	27 027	n.d.		126	<sup>5</sup> L	7	E	29 592	n.d.	
60	<sup>5</sup> L	10	A <sub>2</sub>	27 068	n.d.		127	<sup>5</sup> L	6	E	29 612	n.d.	
61	<sup>5</sup> L	10	A <sub>1</sub>	27 086	n.d.		128	<sup>5</sup> L	7	A <sub>2</sub>	29 646	n.d.	
62	<sup>5</sup> L	10	A <sub>2</sub>	27 094	n.d.		129	<sup>5</sup> L	6	E	29 729	n.d.	
63	<sup>5</sup> L	10	A <sub>1</sub>	27 096	n.d.		130	<sup>5</sup> L	6	E	29 747	n.d.	
64	<sup>5</sup> L	10	E	27 152	n.d.		131	<sup>5</sup> L	6	A <sub>2</sub>	29 748	n.d.	
65	<sup>5</sup> L	10	E	27 163	n.d.		132	<sup>5</sup> L	6	A <sub>1</sub>	29 771	n.d.	
66	<sup>5</sup> L	10	E	27 214	n.d.		133	<sup>5</sup> L	6	E	29 861	n.d.	
67	<sup>5</sup> L	10	A <sub>1</sub>	27 234	n.d.		134	<sup>5</sup> L	6	A <sub>1</sub>	29 891	n.d.	

Table 2 (Continued)

level no.	term <sup>a</sup>	J <sup>a</sup>	Γ <sup>b</sup>	energy (cm <sup>-1</sup> )			level no.	term <sup>a</sup>	J <sup>a</sup>	Γ <sup>b</sup>	energy (cm <sup>-1</sup> )		
				calc <sup>c</sup>	expt <sup>d</sup>	Δ <sup>e</sup>					calc <sup>c</sup>	expt <sup>d</sup>	Δ <sup>e</sup>
135	<sup>5</sup> D (3)	1	E	30 659	30 653	6	204	<sup>5</sup> I (2)	7	E	36 573	n.d.	
136	<sup>5</sup> D (3)	1	A <sub>2</sub>	30 668	30 671	-3	205	<sup>5</sup> I (2)	7	A <sub>2</sub>	36 575	36 566	9
137	<sup>5</sup> H (1)	7	A <sub>2</sub>	31 268	31 249	19	206	<sup>5</sup> I (2)	7	A <sub>1</sub>	36 582	n.d.	
138	<sup>5</sup> D (3)	0	A <sub>1</sub>	31 283	n.d.		207	<sup>5</sup> I (2)	7	E	36 583	36 579	4
139	<sup>5</sup> H (1)	7	E	31 287	n.d.		208	<sup>5</sup> I (2)	7	E	36 587	n.d.	
140	<sup>5</sup> H (1)	7	E	31 346	31 345	1	209	<sup>5</sup> I (2)	7	A <sub>2</sub>	36 592	n.d.	
141	<sup>5</sup> H (1)	7	E	31 355	n.d.		210	<sup>5</sup> I (2)	7	E	36 610	n.d.	
142	<sup>5</sup> H (1)	7	A <sub>2</sub>	31 363	31 364	-1	211	<sup>5</sup> I (2)	7	A <sub>1</sub>	36 611	n.d.	
143	<sup>5</sup> H (1)	7	A <sub>1</sub>	31 366	n.d.		212	<sup>5</sup> I (2)	7	E	36 620	n.d.	
144	<sup>5</sup> H (1)	7	A <sub>2</sub>	31 444	31 442	2	213	<sup>5</sup> I (2)	7	A <sub>2</sub>	36 658	n.d.	
145	<sup>5</sup> H (1)	7	A <sub>1</sub>	31 453	n.d.		214	<sup>5</sup> F (2)	2	E	37 052	n.d.	
146	<sup>5</sup> H (1)	7	E	31 456	n.d.		215	<sup>5</sup> F (2)	2	E	37 074	n.d.	
147	<sup>5</sup> H (1)	7	E	31 471	31 477	-6	216	<sup>5</sup> F (2)	2	A <sub>1</sub>	37 079	n.d.	
148	<sup>5</sup> H (1)	6	A <sub>1</sub>	32 766	n.d.		217	<sup>5</sup> F (2)	1	E	37 350	n.d.	
149	<sup>5</sup> H (1)	6	E	32 796	n.d.		218	<sup>5</sup> F (2)	1	A <sub>2</sub>	37 358	n.d.	
150	<sup>5</sup> H (1)	6	E	32 851	32 848	3	219	<sup>5</sup> I (2)	4	E	37 476	n.d.	
151	<sup>5</sup> H (1)	6	A <sub>2</sub>	32 864	32 860	4	220	<sup>5</sup> I (2)	4	A <sub>2</sub>	37 511	n.d.	
152	<sup>5</sup> H (1)	6	A <sub>1</sub>	32 893	n.d.		221	<sup>5</sup> I (2)	6	E	37 537	n.d.	
153	<sup>5</sup> H (1)	6	E	32 911	32 922	-11	222	<sup>5</sup> I (2)	6	A <sub>1</sub>	37 554	n.d.	
154	<sup>5</sup> H (1)	6	A <sub>1</sub>	32 940	n.d.		223	<sup>5</sup> I (2)	6	A <sub>1</sub>	37 567	n.d.	
155	<sup>5</sup> H (1)	6	E	32 950	32 964	-14	224	<sup>5</sup> I (2)	4	E	37 575	37 580	-5
156	<sup>5</sup> H (1)	6	A <sub>2</sub>	32 982	32 983	-1	225	<sup>5</sup> I (2)	6	A <sub>1</sub>	37 585	n.d.	
157	<sup>5</sup> H (1)	5	A <sub>2</sub>	33 670	n.d.		226	<sup>5</sup> I (2)	6	E	37 590	n.d.	
158	<sup>5</sup> H (1)	5	E	33 690	33 690	0	227	<sup>5</sup> I (2)	6	E	37 605	n.d.	
159	<sup>5</sup> H (1)	5	E	33 745	n.d.		228	<sup>5</sup> I (2)	6	A <sub>1</sub>	37 612	n.d.	
160	<sup>5</sup> H (1)	5	E	33 762	n.d.		229	<sup>5</sup> I (2)	6	A <sub>2</sub>	37 617	n.d.	
161	<sup>5</sup> H (1)	5	E	33 780	33 788	-8	230	<sup>5</sup> I (2)	6	E	37 636	n.d.	
162	<sup>5</sup> H (1)	5	A <sub>2</sub>	33 781	n.d.		231	<sup>5</sup> I (2)	6	A <sub>2</sub>	37 669	n.d.	
163	<sup>5</sup> H (1)	5	A <sub>1</sub>	33 799	n.d.		232	<sup>5</sup> I (2)	4	E	37 677	n.d.	
164	<sup>5</sup> H (1)	4	E	34 271	n.d.		233	<sup>5</sup> I (2)	4	A <sub>1</sub>	37 719	n.d.	
165	<sup>5</sup> H (1)	4	A <sub>1</sub>	34 285	n.d.		234	<sup>5</sup> I (2)	5	A <sub>2</sub>	37 965	n.d.	
166	<sup>5</sup> H (1)	4	E	34 321	n.d.		235	<sup>5</sup> I (2)	5	E	37 966	n.d.	
167	<sup>5</sup> H (1)	4	A <sub>2</sub>	34 322	n.d.		236	<sup>5</sup> I (2)	5	A <sub>1</sub>	37 969	n.d.	
168	<sup>5</sup> H (1)	4	E	34 331	n.d.		237	<sup>5</sup> I (2)	5	E	37 986	n.d.	
169	<sup>5</sup> H (1)	4	A <sub>1</sub>	34 342	n.d.		238	<sup>5</sup> I (2)	5	A <sub>2</sub>	37 998	n.d.	
170	<sup>5</sup> H (1)	3	A <sub>2</sub>	34 807	n.d.		239	<sup>5</sup> I (2)	5	E	38 005	n.d.	
171	<sup>5</sup> F (2)	5	E	34 822	34 809	13	240	<sup>5</sup> I (2)	5	E	38 010	n.d.	
172	<sup>5</sup> F (2)	5	A <sub>2</sub>	34 844	34 846	-1	241	<sup>5</sup> K	9	A <sub>2</sub>	39 009	38 990	19
173	<sup>5</sup> F (2)	5	E	34 851	n.d.		242	<sup>5</sup> K	9	E	39 023	39 027	-4
174	<sup>5</sup> F (2)	5	A <sub>2</sub>	34 897	n.d.		243	<sup>5</sup> K	9	E	39 050	n.d.	
175	<sup>5</sup> H (1)	3	E	34 904	n.d.		244	<sup>5</sup> K	9	A <sub>2</sub>	39 070	n.d.	
176	<sup>5</sup> F (2)	5	E	34 911	n.d.		245	<sup>5</sup> K	9	A <sub>1</sub>	39 082	n.d.	
177	<sup>5</sup> F (2)	5	A <sub>2</sub>	34 942	n.d.		246	<sup>5</sup> K	9	E	39 130	n.d.	
178	<sup>5</sup> H (1)	3	A <sub>1</sub>	34 946	n.d.		247	<sup>5</sup> K	9	E	39 151	n.d.	
179	<sup>5</sup> F (2)	5	A <sub>1</sub>	34 949	n.d.		248	<sup>5</sup> K	9	A <sub>2</sub>	39 163	n.d.	
180	<sup>5</sup> H (1)	3	E	34 968	n.d.		249	<sup>5</sup> K	9	A <sub>1</sub>	39 199	n.d.	
181	<sup>5</sup> H (1)	3	E	35 033	35 031	2	250	<sup>5</sup> K	9	E	39 255	n.d.	
182	<sup>5</sup> I (2)	8	E	35 048	35 046	2	251	<sup>5</sup> K	9	A <sub>1</sub>	39 257	n.d.	
183	<sup>5</sup> I (2)	8	E	35 059	n.d.		252	<sup>5</sup> K	9	A <sub>2</sub>	39 266	n.d.	
184	<sup>5</sup> I (2)	8	A <sub>2</sub>	35 063	n.d.		253	<sup>5</sup> K	9	E	39 269	n.d.	
185	<sup>5</sup> I (2)	8	A <sub>1</sub>	35 097	n.d.		254	<sup>5</sup> D (2)	2	A <sub>1</sub>	39 318	n.d.	
186	<sup>5</sup> I (2)	8	E	35 113	35 107	6	255	<sup>5</sup> D (2)	2	E	39 319	39 346	-27
187	<sup>5</sup> I (2)	8	E	35 136	n.d.		256	<sup>5</sup> D (2)	2	E	39 337	39 368	-31
188	<sup>5</sup> I (2)	8	A <sub>2</sub>	35 139	n.d.		257	<sup>5</sup> K	6	A <sub>2</sub>	40 048	n.d.	
189	<sup>5</sup> I (2)	8	A <sub>1</sub>	35 142	n.d.		258	<sup>5</sup> K	6	E	40 098	n.d.	
190	<sup>5</sup> I (2)	8	E	35 179	n.d.		259	<sup>5</sup> K	6	A <sub>1</sub>	40 102	n.d.	
191	<sup>5</sup> I (2)	8	E	35 187	35 186	1	260	<sup>5</sup> K	6	E	40 129	n.d.	
192	<sup>5</sup> I (2)	8	A <sub>1</sub>	35 196	n.d.		261	<sup>5</sup> K	6	A <sub>1</sub>	40 146	n.d.	
193	<sup>5</sup> F (2)	4	E	35 334	35 338	-4	262	<sup>5</sup> K	6	A <sub>2</sub>	40 177	n.d.	
194	<sup>5</sup> F (2)	4	A <sub>1</sub>	35 335	n.d.		263	<sup>5</sup> K	6	E	40 182	n.d.	
195	<sup>5</sup> F (2)	4	E	35 371	35 366	5	264	<sup>5</sup> K	6	E	40 246	n.d.	
196	<sup>5</sup> F (2)	4	E	35 389	n.d.		265	<sup>5</sup> K	6	A <sub>1</sub>	40 291	n.d.	
197	<sup>5</sup> F (2)	4	A <sub>2</sub>	35 392	n.d.		266	<sup>5</sup> K	8	A <sub>1</sub>	40 674	n.d.	
198	<sup>5</sup> F (2)	4	A <sub>1</sub>	35 411	n.d.		267	<sup>5</sup> K	8	E	40 694	n.d.	
199	<sup>5</sup> F (2)	3	A <sub>1</sub>	36 411	n.d.		268	<sup>5</sup> K	8	E	40 713	n.d.	
200	<sup>5</sup> F (2)	3	A <sub>2</sub>	36 436	n.d.		269	<sup>5</sup> K	8	E	40 731	n.d.	
201	<sup>5</sup> F (2)	3	E	36 458	n.d.		270	<sup>5</sup> K	8	A <sub>2</sub>	40 748	n.d.	
202	<sup>5</sup> F (2)	3	A <sub>2</sub>	36 478	n.d.		271	<sup>5</sup> K	8	A <sub>1</sub>	40 755	n.d.	
203	<sup>5</sup> F (2)	3	E	36 494	36 494	0	272	<sup>5</sup> K	8	E	40 758	n.d.	

Table 2 (Continued)

level no.	term <sup>a</sup>	J <sup>a</sup>	Γ <sup>b</sup>	energy (cm <sup>-1</sup> )			level no.	term <sup>a</sup>	J <sup>a</sup>	Γ <sup>b</sup>	energy (cm <sup>-1</sup> )		
				calc <sup>c</sup>	expt <sup>d</sup>	Δ <sup>e</sup>					calc <sup>c</sup>	expt <sup>d</sup>	Δ <sup>e</sup>
273	<sup>5</sup> K	8	E	40 821	n.d.		293	<sup>5</sup> K	7	E	41 574	n.d.	
274	<sup>5</sup> K	8	A <sub>2</sub>	40 822	n.d.		294	<sup>5</sup> K	7	A <sub>2</sub>	41 600	n.d.	
275	<sup>5</sup> K	8	E	40 831	n.d.		295	<sup>5</sup> K	7	E	41 605	n.d.	
276	<sup>5</sup> K	8	A <sub>1</sub>	40 842	n.d.		296	<sup>5</sup> K	7	A <sub>1</sub>	41 619	n.d.	
277	<sup>5</sup> G (2)	6	E	41 200	n.d.		297	<sup>5</sup> K	7	A <sub>2</sub>	41 624	n.d.	
278	<sup>5</sup> G (2)	6	E	41 211	n.d.		298	<sup>5</sup> K	7	E	41 632	n.d.	
279	<sup>5</sup> K	5	A <sub>2</sub>	41 220	n.d.		299	<sup>5</sup> K	7	E	41 680	n.d.	
280	<sup>5</sup> K	5	E	41 231	41 235	-4	300	<sup>5</sup> K	7	A <sub>1</sub>	41 693	n.d.	
281	<sup>5</sup> G (2)	6	A <sub>1</sub>	41 236	n.d.		301	<sup>5</sup> K	7	A <sub>2</sub>	41 695	n.d.	
282	<sup>5</sup> K	5	E	41 258	n.d.		302	<sup>5</sup> K	7	E	41 699	n.d.	
283	<sup>5</sup> K	5	A <sub>1</sub>	41 283	n.d.		303	<sup>5</sup> D (2)	3	A <sub>2</sub>	42 003	n.d.	
284	<sup>5</sup> K	5	E	41 284	n.d.		304	<sup>5</sup> D (2)	3	A <sub>1</sub>	42 075	n.d.	
285	<sup>5</sup> K	5	A <sub>2</sub>	41 285	n.d.		305	<sup>5</sup> D (2)	3	E	42 078	n.d.	
286	<sup>5</sup> K	5	A <sub>2</sub>	41 306	n.d.		306	<sup>5</sup> D (2)	3	A <sub>2</sub>	42 119	42 102	17
287	<sup>5</sup> K	5	E	41 315	n.d.		307	<sup>5</sup> D (2)	3	E	42 142	n.d.	
288	<sup>5</sup> K	5	A <sub>1</sub>	41 338	n.d.		308	<sup>5</sup> G (2)	5	E	42 319	42 303	16
289	<sup>5</sup> K	5	E	41 361	n.d.		309	<sup>5</sup> G (2)	5	A <sub>2</sub>	42 322	n.d.	
290	<sup>5</sup> K	5	A <sub>2</sub>	41 369	n.d.		310	<sup>5</sup> G (2)	5	E	42 329	n.d.	
291	<sup>5</sup> K	5	E	41 370	n.d.		311	<sup>5</sup> G (2)	5	E	42 359	42 353	6
292	<sup>5</sup> K	5	A <sub>1</sub>	41 372	n.d.		312	<sup>5</sup> G (2)	5	A <sub>2</sub>	42 371	n.d.	
							313	<sup>5</sup> G (2)	5	A <sub>1</sub>	42 372	n.d.	
							314	<sup>5</sup> G (2)	5	E	42 386	n.d.	

<sup>a</sup> Identifies the *principal* SLJ components of the eigenvectors. <sup>b</sup> Irreducible representation (irrep) label in *D*<sub>3</sub> point group. <sup>c</sup> Calculated by using the Hamiltonian parameter values listed in Table 3. <sup>d</sup> Experimentally determined locations of energy levels, with 1/λ(air) to 1/λ(vacuum) corrections included. Uncertainties in the energy–level locations are ca. ±3 cm<sup>-1</sup> (on average). n.d. ≡ not determined (i.e., energy level not fully characterized with respect to location and/or symmetry type). <sup>e</sup> Difference between calculated and observed energies.

Table 3. Energy Parameters for the 4f<sup>8</sup> Electronic Configuration of Tb<sup>3+</sup> in Na<sub>3</sub>[Tb(oda)<sub>3</sub>]·2NaClO<sub>4</sub>·6H<sub>2</sub>O

parameter <sup>a</sup>	value <sup>b</sup> /cm <sup>-1</sup>	parameter <sup>a</sup>	value <sup>b</sup> /cm <sup>-1</sup>
<i>E</i> <sub>av</sub>	68 195(7)	<i>M</i> <sup>0</sup>	1.95(0.07)
<i>F</i> <sup>2</sup>	90 251(25)	<i>M</i> <sup>2</sup>	0.56 <i>M</i> <sup>0</sup>
<i>F</i> <sup>4</sup>	64 414(48)	<i>M</i> <sup>4</sup>	0.38 <i>M</i> <sup>0</sup>
<i>F</i> <sup>6</sup>	43 627(53)	<i>P</i> <sup>2</sup>	[373]
ζ <sub>so</sub>	1700(2)	<i>P</i> <sup>4</sup>	[186]
α	18.6(0.1)	<i>P</i> <sup>6</sup>	[37]
β	-643(17)	<i>B</i> <sub>0</sub> <sup>2</sup>	51(41)
γ	[1652]	<i>B</i> <sub>0</sub> <sup>4</sup>	-955(57)
<i>T</i> <sup>2</sup>	[320]	<i>B</i> <sub>3</sub> <sup>4</sup>	-791(41)
<i>T</i> <sup>3</sup>	[40]	<i>B</i> <sub>0</sub> <sup>6</sup>	-664(90)
<i>T</i> <sup>4</sup>	[50]	<i>B</i> <sub>3</sub> <sup>6</sup>	-1048(57)
<i>T</i> <sup>6</sup>	[-395]	<i>B</i> <sub>6</sub> <sup>6</sup>	-877(51)
<i>T</i> <sup>7</sup>	[303]		
<i>T</i> <sup>8</sup>	[317]	<i>N</i> <sup>c</sup>	95
		<i>σ</i> <sup>d</sup>	11.7

<sup>a</sup> Defined according to eqs 2 and 4. <sup>b</sup> Determined from parametric fits of the experimentally observed energy-level data listed in Table 2. The numbers shown in parentheses represent uncertainties in the parameter values and correspond to the (±) changes in parameter values that produce a doubling of the *variance* obtained in the data fits. The parameter values shown in square brackets were held fixed in performing the data fits. <sup>c</sup> Number of assigned energy levels included in the parametric data fits. <sup>d</sup> Root-mean-square deviation between calculated and observed energies (in cm<sup>-1</sup>).

The atomic Hamiltonian used in the present study may be written in the following parametrized form:

$$\hat{H}_a = E_{av} + \sum_k F^k \hat{t}_k + \alpha \hat{L}(\hat{L} + 1) + \beta \hat{G}(G_2) + \gamma \hat{G}(R_7) + \sum_i T^i \hat{t}_i + \zeta_{so} \hat{A}_{so} + \sum_k P^k \hat{p}_k + \sum_j M^j \hat{m}_j \quad (2)$$

where *k* = 2, 4, 6; *i* = 2, 3, 4, 6, 7, 8; *j* = 0, 2, 4; and each of the interaction operators and parameters is written and defined according to conventional practice.<sup>34,35</sup> Defined according to eq 2, the  $\hat{H}_a$  operator

Table 4. Comparisons of Crystal-Field Parameters and Interaction Strengths Reported for Tb<sup>3+</sup> in Three Crystal Systems Having Trigonal Site Symmetries<sup>a</sup>

parameter <sup>b</sup>	TbODA ( <i>D</i> <sub>3</sub> ) <sup>c</sup>	Yb <sub>0.95</sub> Tb <sub>0.05</sub> DPA ( <i>D</i> <sub>3</sub> ) <sup>d</sup>	Tb <sup>3+</sup> :LaCl <sub>3</sub> ( <i>C</i> <sub>3<i>m</i></sub> ) <sup>e</sup>
<i>B</i> <sub>0</sub> <sup>2</sup>	51	-140	184
<i>B</i> <sub>0</sub> <sup>4</sup>	-955	-325	-295
<i>B</i> <sub>3</sub> <sup>4</sup>	-791	-365	
<i>B</i> <sub>0</sub> <sup>6</sup>	-664	-610	-459
<i>B</i> <sub>3</sub> <sup>6</sup>	-1048	-611	
<i>B</i> <sub>6</sub> <sup>6</sup>	-877	-898	284
<i>S</i> <sub>cf</sub> <sup>2</sup>	23	63	82
<i>S</i> <sub>cf</sub> <sup>4</sup>	490	203	98
<i>S</i> <sub>cf</sub> <sup>6</sup>	567	458	169
<i>S</i> <sub>cf</sub>	433	292	122

<sup>a</sup> All parameter values are given in units of cm<sup>-1</sup>. <sup>b</sup> The *B*<sub>*m*</sub><sup>*k*</sup> crystal-field parameters are defined according to eq 3 in text. The *S*<sub>cf</sub><sup>*k*</sup> and *S*<sub>cf</sub> crystal-field *strength* parameters are defined according to eqs 5 and 6 in the text. <sup>c</sup> From present work. <sup>d</sup> From ref 33. <sup>e</sup> From ref 38.

contains 20 parameters (including *E*<sub>av</sub>). Implicit in these parameters are the radial-coordinate-dependent parts of the interactions represented in  $\hat{H}_a$ .

The even-parity crystal-field Hamiltonian,  $\hat{H}_{cf}^+$ , is defined to reflect the *D*<sub>3</sub> point symmetry at the Tb<sup>3+</sup> sites in TbODA and is expressed here as

$$\hat{H}_{cf}^+ = \sum_{k,m} B_m^k \hat{C}_m^{(k)} \quad (3)$$

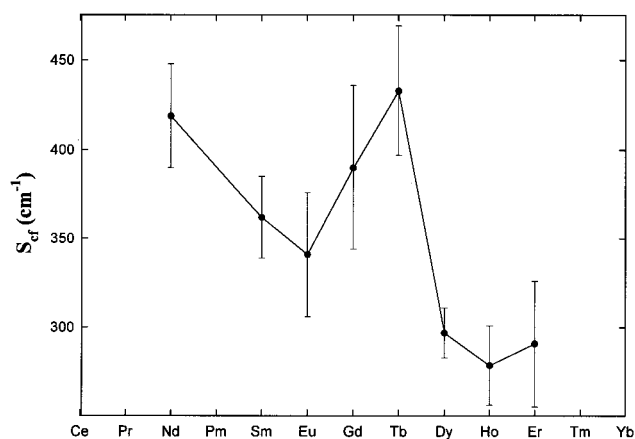
where *k* = 2, 4, 6; *m* = 0, ±3, ±6 (with |*m*| ≤ *k*);  $\hat{C}_m^{(k)}$  is a many-electron spherical-tensor operator (of rank *k* and order *m*) that acts within the 4f<sup>8</sup>(Tb<sup>3+</sup>) electronic configuration; and the *B*<sub>*m*</sub><sup>*k*</sup> are crystal-field interaction parameters. The *B*<sub>*m*</sub><sup>*k*</sup> parameters in eq 3 are interrelated according to *B*<sub>-*m*</sub><sup>*k*</sup> = (-1)<sup>*m*</sup>*B*<sub>*m*</sub><sup>*k*</sup>, and, therefore, the  $\hat{H}_{cf}^+$  operator may be reexpressed as

- (34) Crosswhite, H. M.; Crosswhite, H. *J. Opt. Soc. Am. B* **1984**, *1*, 246.  
 (35) Carnall, W. T.; Goodman, G. L.; Rajnak, K.; Rana, R. S. *J. Chem. Phys.* **1989**, *90*, 3443.

**Table 5.** Comparisons of Crystal-Field Parameters and Interaction Strengths Determined for Eight Na<sub>3</sub>[Ln(oda)<sub>3</sub>]·2NaClO<sub>4</sub>·6H<sub>2</sub>O Systems<sup>a</sup>

parameter <sup>b</sup>	values/cm <sup>-1</sup>							
	NdODA <sup>c</sup>	SmODA <sup>d</sup>	EuODA <sup>e</sup>	GdODA <sup>f</sup>	TbODA <sup>g</sup>	DyODA <sup>h</sup>	HoODA <sup>i</sup>	ErODA <sup>j</sup>
$B_0^2$	-41(20)	13(26)	67(43)	63(10)	51(41)	59(13)	64(23)	65(31)
$B_0^4$	-985(53)	-834(44)	-839(60)	-844(32)	-955(57)	-755(25)	-741(38)	-781(69)
$B_3^4$	-836(32)	-742(27)	-692(41)	-749(12)	-791(41)	-588(21)	-512(28)	-660(50)
$B_0^6$	-452(59)	-474(42)	-322(61)	-629(265)	-664(90)	-393(27)	-416(48)	-293(49)
$B_3^6$	-1063(41)	-871(31)	-810(53)	-937(81)	-1048(57)	-620(17)	-608(31)	-517(38)
$B_6^6$	-694(53)	-622(34)	-591(57)	-752(19)	-877(51)	-581(16)	-526(31)	-507(29)
$S_{cf}^2$	18(9)	6(12)	30(19)	28(4)	23(18)	26(6)	29(10)	29(14)
$S_{cf}^4$	513(16)	447(14)	430(20)	451(8)	490(19)	374(9)	345(13)	406(23)
$S_{cf}^6$	513(18)	440(12)	403(21)	503(35)	567(22)	351(7)	336(12)	296(13)
$S_{cf}$	419(29)	362(23)	341(35)	390(46)	433(36)	297(14)	279(22)	291(35)
$N$	116	144	61	60	95	152	105	65
$\sigma$	14.4	12.3	9.9	6.3	11.7	8.2	9.1	9.6

<sup>a</sup> Determined from parametric analyses of empirical energy-level data.  $N$  = number of assigned energy levels included in the data fits.  $\sigma$  = rms deviation between calculated and observed energies (expressed in cm<sup>-1</sup>). <sup>b</sup> The  $B_m^k$  crystal-field parameters are defined according to eq 4 in the text. The  $S_{cf}^k$  and  $S_{cf}$  are defined according to eqs 5 and 6 in the text. <sup>c</sup> From ref 8. <sup>d</sup> From ref 12. <sup>e</sup> From ref 16. and J. Quagliano (University of Virginia), unpublished results. <sup>f</sup> From ref 21. <sup>g</sup> From present work. <sup>h</sup> From ref 24. <sup>i</sup> From ref 25. <sup>j</sup> From ref 28.



**Figure 1.** Plot of the crystal-field interaction strength ( $S_{cf}$ ) quantities determined for eight LnODA systems. Connecting lines between adjacent points are included for clarity.

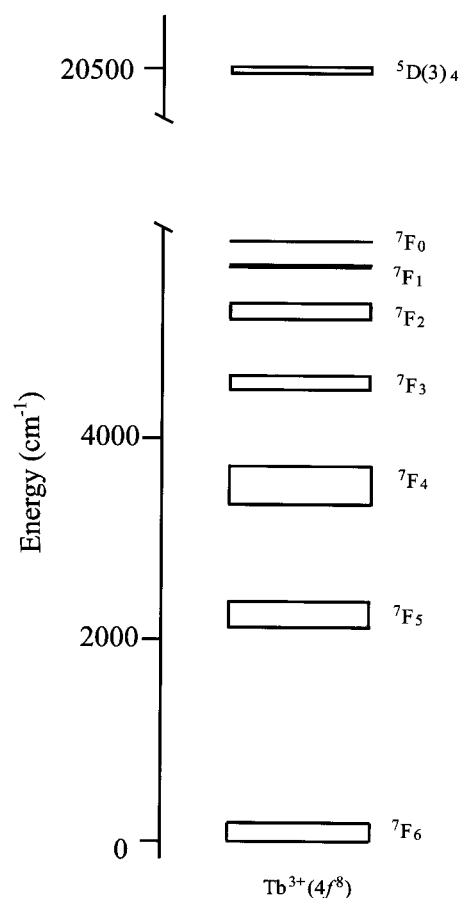
$$\hat{H}_{cf}^+ = B_0^2 \hat{C}_0^{(2)} + B_0^4 \hat{C}_0^{(4)} + B_3^4 (\hat{C}_3^{(4)} - \hat{C}_{-3}^{(4)}) + B_0^6 \hat{C}_0^{(6)} + B_3^6 (\hat{C}_3^{(6)} - \hat{C}_{-3}^{(6)}) + B_6^6 (\hat{C}_6^{(6)} + \hat{C}_{-6}^{(6)}) \quad (4)$$

which contains just six independent crystal-field interaction parameters.

Our energy-level calculations were carried out in two steps. In the first step the atomic Hamiltonian was diagonalized within the complete set of  $f^8 \text{SM}_3 \text{LM}_L$  angular-momentum states with the parameters of  $\hat{H}_a$  fixed at the values reported previously for Tb<sup>3+</sup> in LaF<sub>3</sub>.<sup>35</sup> The 740 lowest-energy  $f^8[\text{SL}]M_J$  intermediate-coupled states derived from this calculation were then used as the basis set in our calculations of crystal-field energy-level structure. In these latter calculations, the complete model Hamiltonian ( $\hat{H} = \hat{H}_a + \hat{H}_{cf}^+$ ) was diagonalized within the  $f^8[\text{SL}]M_J$  basis with 14 of the 26 parameters in our model Hamiltonian ( $\hat{H} = \hat{H}_a + \hat{H}_{cf}^+$ ) treated as variables to fit calculated energy levels to experimentally observed energy-level data. The parameters treated as variables in the calculations included all six  $B_m^k$  crystal-field parameters and 8 of the 20 atomic Hamiltonian parameters ( $E_{av}$ ,  $F^{2,4,6}$ ,  $\alpha$ ,  $\beta$ ,  $\zeta_{so}$ ,  $M^0$ ). The  $T^i$  ( $i = 2, 3, 4, 6, 7, 8$ ),  $\gamma$ , and  $P^{2,4,6}$  parameters were assigned fixed values taken from a previous analysis of  $4f^8(\text{Tb}^{3+})$  in LaF<sub>3</sub>.<sup>35</sup> The  $M^2$  and  $M^4$  parameters were constrained according to the following relationships:  $M^2 = 0.56M^0$  and  $M^4 = 0.38M^0$ , with  $M^0$  treated as a free variable in performing the data fits. Both the energies and symmetries of crystal-field levels were considered in performing these parametric data fits.

## Results and Discussion

**Energy Levels.** The energy levels located and assigned from our optical and chiroptical measurements on TbODA are shown



**Figure 2.** Energy diagram showing the locations and widths of the eight lowest-energy  $4f^8[\text{SL}]J$  multiplet manifolds of Tb<sup>3+</sup> in TbODA. See Table 2 for greater detail.

in Table 2, along with a listing of all calculated energy levels between 0 and 42 400 cm<sup>-1</sup>. The levels are characterized with respect to their principal  $2S+1L$  term and  $J$  multiplet parentages, their crystal-field symmetry label ( $\Gamma \equiv A_1, A_2, \text{ or } E$ ) in the  $D_3$  point group, and their observed and/or calculated energies. The calculated levels listed in Table 2 were obtained using the Hamiltonian parameter values shown in Table 3. The latter were derived from parametric fits of calculated-to-observed energy-level data. The number of observed levels included in these data fits was 95, and the number of Hamiltonian parameters allowed to freely vary in performing the final data fits was 14.

The parameter values shown inside square brackets in the Table 3 listing were held fixed in carrying out the final data fits. The empirical data set was too small and spanned too few of the  $^{2S+1}L_J$  multiplet manifolds to permit a more thorough exploration of the overall atomic Hamiltonian parameter space.

The 95 experimental levels listed in Table 2 span the 46 lowest-energy  $^{2S+1}L_J$  multiplet manifolds of  $4f^8(\text{Tb}^{3+})$ . Many more of the 314 levels falling within the spectral range of our measurements ( $0\text{--}42\,550\text{ cm}^{-1}$ ) were located but could not be unambiguously characterized with respect to symmetry. Only the 95 fully assigned levels were used in our energy-level data fits. The root-mean-square (rms) deviation between the calculated and observed energies of these 95 assigned levels is  $11.7\text{ cm}^{-1}$ . The overall quality of the energy-level data fit is reasonably good, particularly for an electronic state structure as complex as that of  $4f^8(\text{Tb}^{3+})$  in TbODA. However, an unresolved problem remains in the calculated orderings of the three lowest crystal-field levels split out of the  $^5D(3)_4$  multiplet, and our fits of the energy-level structures observed within several of the  $^7F_J$  multiplet manifolds show rms deviations  $>13\text{ cm}^{-1}$  (but in all cases  $<18\text{ cm}^{-1}$ ). All attempts to fix these problems by making surgical adjustments in selected parameters of the model Hamiltonian either failed to resolve the problems or led to a significant degradation in the quality of the overall data fits. The discrepancies between calculated and experimentally observed energy-level orderings in  $^5D(3)_4$  are especially troublesome because each of the levels in question may be expected to make contributions to the emission spectra measured in this study. Our calculations show the following locations and symmetry assignments for the three lowest crystal-field levels of  $^5D(3)_4$ : an  $A_1$  level at  $20\,444\text{ cm}^{-1}$ ; an  $A_2$  level at  $20\,467\text{ cm}^{-1}$ ; and an E level at  $20\,468\text{ cm}^{-1}$ . However, both our absorption and emission spectra measurements indicate that an E level lies lowest (at  $20\,462\text{ cm}^{-1}$ ) and an  $A_2$  level is located at  $20\,468\text{ cm}^{-1}$ , but these measurements fail to locate the predicted low-lying  $A_1$  level. It is possible, of course, that this  $A_1$  level does in fact lie lowest in energy but does not participate in any optical transitions detectable in our experiments.

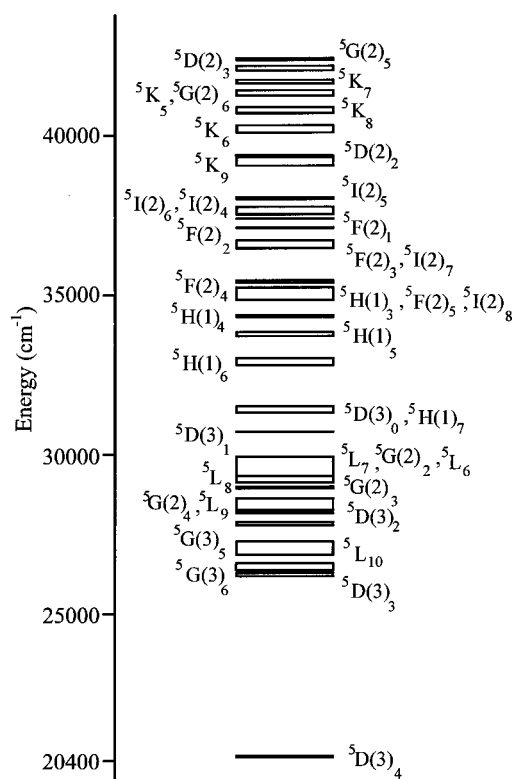
**Comparisons of Crystal Field Parameters and Interaction Strengths.** In Table 4 we show a comparison of the crystal-field interaction parameters ( $B_m^k$ ) determined for  $\text{Tb}^{3+}(4f^8)$  in three different trigonally symmetric systems (including TbODA), and in Table 5 we show a comparison of the crystal-field interaction parameters determined for eight different LnODA systems. All of the  $B_m^k$  parameters given in these tables are defined according to eq 3, with spherical tensor normalization properties. Note, however, that the  $B_3^4$  and  $B_3^6$  parameters vanish in the  $C_{3h}$  site symmetry of  $\text{Tb}^{3+}$  in  $\text{LaCl}_3$ .

Also shown in Tables 4 and 5 are comparisons of the crystal-field interaction strength quantities,  $S_{\text{cf}}^k$  and  $S_{\text{cf}}$ , determined for the various systems. These quantities are defined in terms of the  $B_m^k$  interaction parameters according to

$$S_{\text{cf}}^k = \left( \frac{1}{2k+1} [(B_0^k)^2 + 2 \sum_{m>0} |B_m^k|^2] \right)^{1/2} \quad (5)$$

$$S_{\text{cf}} = \left[ \frac{1}{3} \sum_k (S_{\text{cf}}^k)^2 \right]^{1/2} \quad (6)$$

These interaction strength quantities provide a measure of the extent to which the nonspherically symmetric components of the crystal-field interactions induce  $J$  level mixings and shift



**Figure 3.** Energy diagram showing the locations and widths of all  $4f^8[\text{SL}]J$  multiplet manifolds lying between  $20\,400$  and  $42\,400\text{ cm}^{-1}$  for  $\text{Tb}^{3+}$  in TbODA. See Table 2 for greater detail.

the baricenter energies of  $J$  multiplet manifolds.<sup>36,37</sup> They are frequently used for comparisons of the relative strengths of  $\text{Ln}^{3+}(4f^N)/\text{crystal-field}$  interactions in different host materials.

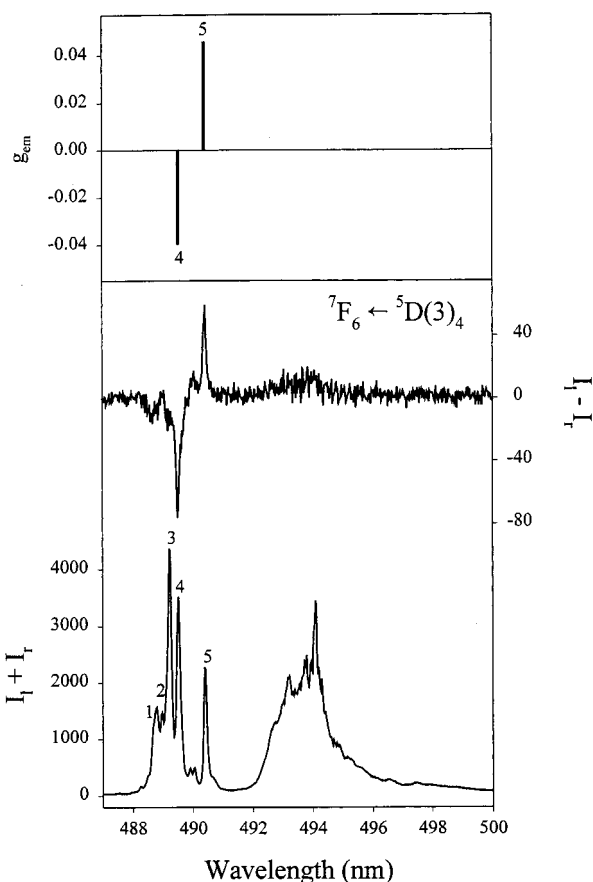
In each of the systems represented in Table 4, the  $\text{Tb}^{3+}$  ions are located at 9-coordinate sites of trigonal symmetry, and in each system the coordination polyhedron formed by the nine ligand donor atoms about each  $\text{Tb}^{3+}$  ion has a slightly distorted tricapped trigonal prism structure. The  $\text{Tb}^{3+}$  donor atom coordination clusters in the respective systems are:  $\text{Tb}^{3+}(\text{Cl}^-)_9$  in  $\text{Tb}^{3+}:\text{LaCl}_3$ ;  $\text{Tb}^{3+}(\text{O}^-)_6(\text{N})_3$  in  $\text{YbTbDPA} \equiv \text{Na}_3[\text{Yb}_{0.95}\text{Tb}_{0.05}(\text{dpa})_3] \cdot \text{NaClO}_4 \cdot 10\text{H}_2\text{O}$ ; and  $\text{Tb}^{3+}(\text{O}^-)_6(\text{O})_3$  in TbODA. In both TbODA and YbTbDPA, the negatively charged oxygen donor atoms are from ligand carboxylate groups and they are located at the vertexes of the trigonal prismatic coordination polyhedron. However, whereas the equatorial (prism-capping) coordination sites in YbTbDPA are occupied by pyridyl nitrogen atoms, these sites are occupied by ether oxygen atoms in TbODA.

The results shown in Table 4 reveal striking differences between the  $\text{Tb}^{3+}(4f^8)/\text{crystal-field}$  interactions in TbODA versus YbTbDPA. These differences are apparent in both the  $B_m^k$  parameter sets and the interaction strength quantities ( $S_{\text{cf}}^k$  and  $S_{\text{cf}}$ ) determined for the respective systems. Except for the interactions represented in  $B_0^2$  and  $B_6^6$ , the crystal-field interactions in TbODA are considerably stronger than those in YbTbDPA, and the  $S_{\text{cf}}$  strength quantity determined for TbODA is nearly 50% greater than that determined for YbTbDPA. This implies that the  $-\text{CH}_2\text{OCH}_2-$  moieties of the  $\text{Tb}(\text{oda})_3^{3-}$  complexes in TbODA exert a much stronger influence on the  $4f^8$  electronic energy-level structure of  $\text{Tb}^{3+}$  than do the pyridyl moieties of the  $\text{Tb}(\text{dpa})_3^{3-}$  complexes in YbTbDPA.

(36) Leavitt, R. P. *J. Chem. Phys.* **1982**, *77*, 1661.

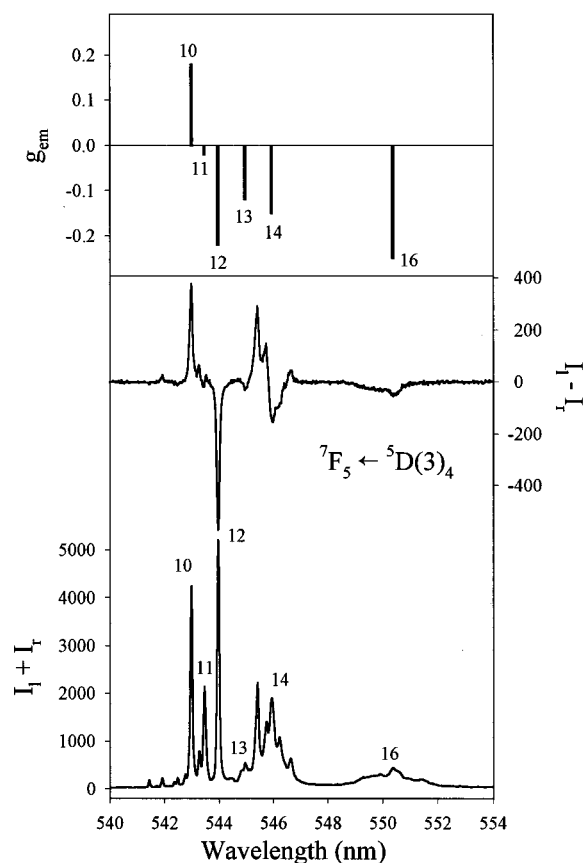
(37) Chang, N. C.; Gruber, J. B.; Leavitt, R. P.; Morrison, C. A. *J. Chem. Phys.* **1982**, *76*, 3877.





**Figure 4.** Spectra obtained from circularly polarized, axial emission measurements in the  ${}^7\text{F}_6 \leftarrow {}^5\text{D}(3)_4$  transition region of  $\text{Tb}^{3+}(4f^8)$  in TbODA. Sample temperature was ca. 20 K, and sample excitation was with the 351–364 nm output of an argon ion laser.

The comparative results shown in Table 5 for LnODA systems exhibit some expected and also some unexpected behavior across the lanthanide series. This is perhaps best demonstrated in the crystal-field interaction strength quantities ( $S_{\text{cf}}$ ) determined for the eight systems. A trans-series plot of  $S_{\text{cf}}$  values is shown in Figure 1. The uncertainty bars in that plot reflect the uncertainties of the  $B_m^k$  parameter values used in calculating the relevant  $S_{\text{cf}}^k$  and  $S_{\text{cf}}$  quantities. We note first that if GdODA and TbODA are excluded from consideration, then the  $S_{\text{cf}}$  values exhibit a reasonably smooth *downward* trend across the series, and this is easily rationalized in terms of the relative radial extent (or spatial diffuseness) of the 4f electron orbitals in the earlier versus later members of the  $\text{Ln}^{3+}$  series. As one progresses across the series (from  $\text{Nd}^{3+}$  to  $\text{Er}^{3+}$ ), the 4f electron charge distributions become more contracted (less diffuse) and, therefore, one expects their interactions with surrounding ligands or crystalline fields to become weaker. Since  $S_{\text{cf}}$  is defined as a measure of crystal-field interaction strength, one would expect a trans-series plot of  $S_{\text{cf}}$  values (for  $\text{Ln}^{3+}$  ions in any given host material) to show a smooth downward trend. The plot shown in Figure 1 conforms with this expectation only if the data points for GdODA and TbODA are excluded from consideration. It is not clear why GdODA and TbODA should show this apparently anomalous behavior in a trans-series comparison of crystal-field interaction strengths. However, it is well-known that in trans- $\text{Ln}^{3+}$ -series comparisons of other physical properties (and some chemical properties), anomalous behavior is often observed for  $\text{Ln}^{3+}$  systems at or near the middle of the series (most often  $\text{Gd}^{3+}$ , but in some cases  $\text{Eu}^{3+}$  and  $\text{Tb}^{3+}$  systems). This is sometimes referred to as the



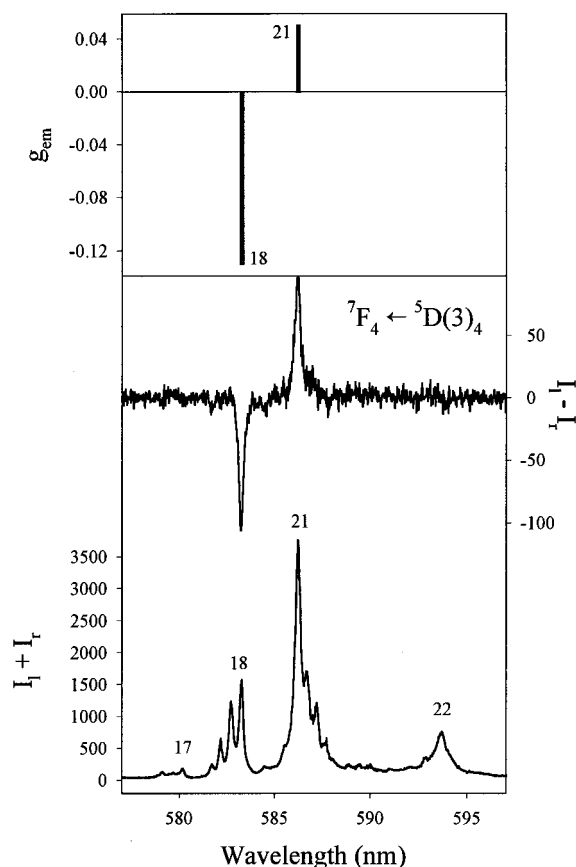
**Figure 5.** Spectra obtained from circularly polarized, axial emission measurements in the  ${}^7\text{F}_5 \leftarrow {}^5\text{D}(3)_4$  transition region of  $\text{Tb}^{3+}(4f^8)$  in TbODA. Sample temperature was ca. 20 K, and sample excitation was with the 488 nm output of an argon ion laser. See text for an explanation of peak numbering.

“gadolinium break” in trans-series comparisons of lanthanide properties, and in a very general sense the results shown in Figure 1 could be placed under this rubric.

**Spectra.** In Figure 2 we show an energy diagram of all the  $J$  multiplet manifolds accessed in our optical emission experiments, and in Figure 3 we show an energy diagram of all the excited  $J$  multiplet manifolds located within the spectral range of our optical absorption measurements (20 400–42 550  $\text{cm}^{-1}$ ). In these figures, the widths shown for the various multiplet manifolds correspond to differences in energy between the highest and lowest crystal-field levels split out of the relevant  $4f^8[\text{SL}]J$  atomic-parentage states, and the locations of the multiplet manifolds are given relative to the lowest-energy crystal-field level of the  ${}^7\text{F}_6$  (ground) multiplet manifold.

The total number of excited  $J$  multiplet manifolds accessible to our absorption spectra measurements was 39, all of which derive principally from Russell–Saunders terms with 5-fold (quintet) spin multiplicity. These multiplet manifolds span the 20 400–42 400  $\text{cm}^{-1}$  energy range (above ground), and they contain a total of 281 crystal-field levels, 140 of which are doubly degenerate (E symmetry in the  $D_3$  point group). Fifty of the E levels were located and assigned from our polarized absorption spectra measurements, and none of these levels showed any evidence of splitting under low-temperature sample conditions (down to ca. 10 K).

Most of the  ${}^7\text{F}_6 \rightarrow$  excited  $J$  multiplet transition regions of  $\text{Tb}^{3+}(4f^8)$  in TbODA exhibit highly congested absorption spectra that are very difficult to deconvolute into lines assignable to individual Stark-level-to-Stark-level transitions of well-defined

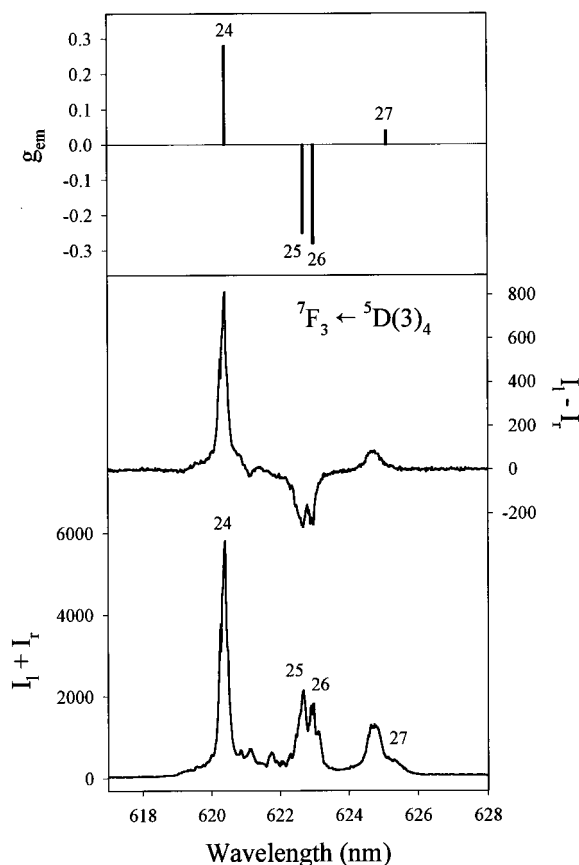


**Figure 6.** Spectra obtained from circularly polarized, axial emission measurements in the  ${}^7F_4 \leftarrow {}^5D(3)_4$  transition region of  $Tb^{3+}(4f^8)$  in TbODA. Sample temperature was ca. 20 K, and sample excitation was with the 488 nm output of an argon ion laser. See text for an explanation of peak numbering.

identities. This is due in large part to the relatively small spacings between the lowest-energy Stark levels of  ${}^7F_6$  and to the high density of Stark levels in many of the excited  $J$  multiplet manifolds. Even spectra obtained at spectral resolutions  $<0.1$  nm, on samples at low temperature, proved difficult to fully assign, in terms of individual Stark-level-to-Stark-level transition components. This accounts in large part for the relatively small number of energy levels (67 total) we list in Table 2 as being fully characterized within the 39 excited  $J$  multiplet manifolds probed in our optical absorption experiments. As was noted earlier, many more levels were located from our absorption (and CD) spectra measurements, but these additional levels could not be unambiguously assigned with respect to symmetry type.

In our previously reported studies of NdODA,<sup>8,9</sup> SmODA,<sup>12–14</sup> EuODA,<sup>16,17</sup> DyODA,<sup>24</sup> and HoODA<sup>25–27</sup> systems, we were able to obtain quantitative absorption line-strength data of sufficient quality and quantity to support detailed theoretical analyses. This was not possible for TbODA because too few lines in the absorption and CD spectra are sufficiently well resolved and characterized to permit quantitative line-strength determination and theoretical analysis. However, some parametric modeling calculations and simulations of polarized line intensity spectra were performed in the present study, using intensity parameters adapted from those derived previously for EuODA,<sup>17</sup> and the results obtained from these modeling exercises proved to be of some value in making line assignments in several difficult-to-interpret transition regions of the absorption spectra.

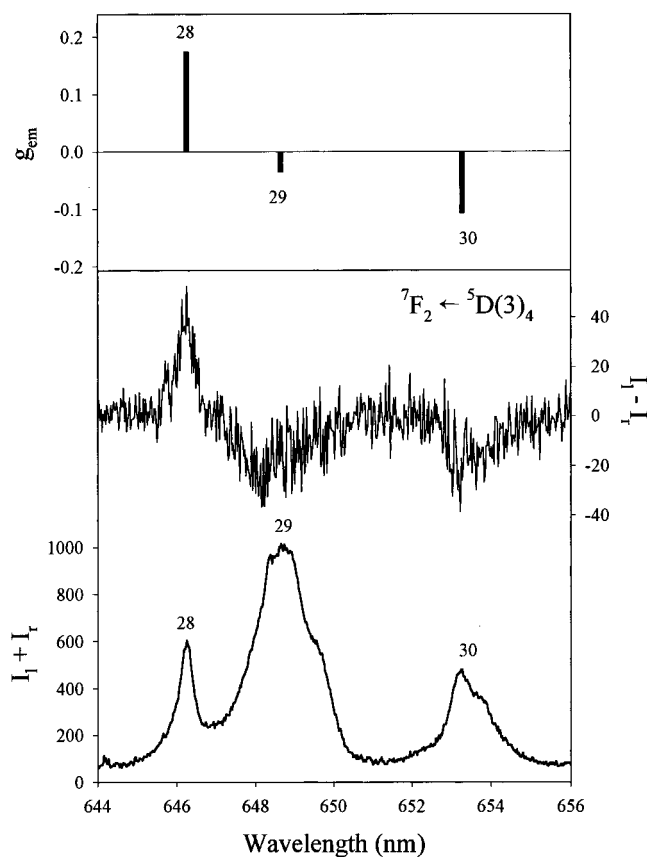
Optical emission spectra measurements were performed throughout each of the  ${}^7F_J (J = 0–6) \leftarrow {}^5D(3)_4$  transition regions



**Figure 7.** Spectra obtained from circularly polarized, axial emission measurements in the  ${}^7F_3 \leftarrow {}^5D(3)_4$  transition region of  $Tb^{3+}(4f^8)$  in TbODA. Sample temperature was ca. 20 K, and sample excitation was with the 488 nm output of an argon ion laser. See text for an explanation of peak numbering.

of  $Tb^{3+}(4f^8)$  in TbODA, and the results obtained from these measurements were used to locate and assign most of the crystal-field levels split out of the  ${}^7F_J$  multiplets. These results were also used, in combination with our absorption measurement data, to characterize the crystal-field energy-level structure of  ${}^5D(3)_4$ . Both circularly polarized (*axial*) and linearly,  $\sigma$  and  $\pi$  polarized (*orthoaxial*) emission measurements proved to be crucial for making line assignments in the emission spectra. Here we will show only a few examples of the spectra obtained, focusing entirely on those in which chiroptical properties are displayed.

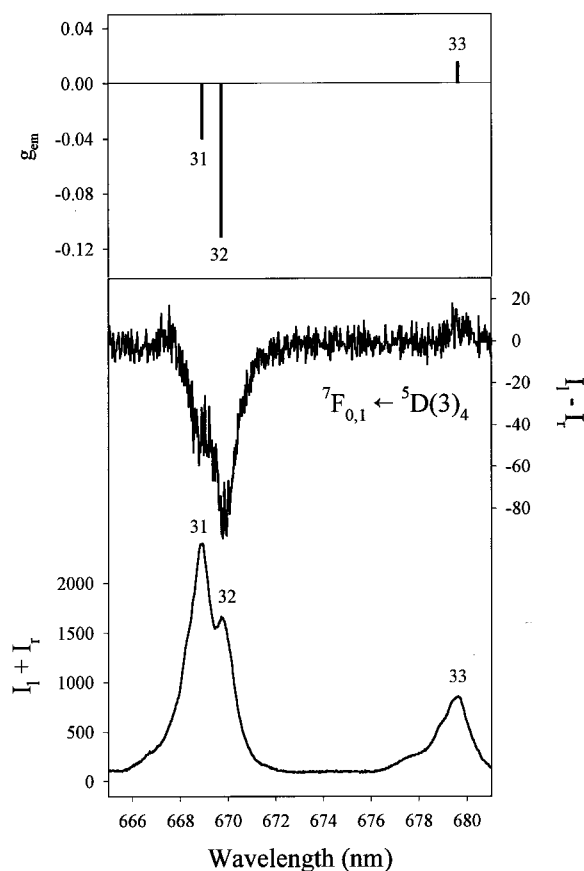
Figures 4–9 show spectra obtained from our measurements of left (l) and right (r) circularly polarized emission intensities ( $I_l$  and  $I_r$ ) throughout the  ${}^7F_J (J = 0–6) \leftarrow {}^5D(3)_4$  transition regions of  $Tb^{3+}(4f^8)$  in TbODA, at a sample temperature of ca. 20 K. The bottom spectrum in each figure is a plot of ( $I_l + I_r$ ) versus emission wavelength, the middle spectrum is a plot of ( $I_l - I_r$ ) versus emission wavelength, and the top, bar spectrum show emission dissymmetry factors,  $g_{em} = 2(I_l - I_r)/(I_l + I_r)$ , measured at several wavelengths in the emission spectra. The spectral features (and bars) labeled with numbers identify the locations of transitions that originate from the lowest E level of  ${}^5D(3)_4$  (i.e., level 34 in Table 2) and terminate on one of the Stark levels of the relevant  ${}^7F_J$  multiplet manifold. The numeric labels on the features identify the terminal levels (according to the level numbers specified in Table 2). None of the spectral features assigned to transitions from higher-lying crystal-field levels of  ${}^5D(3)_4$  (e.g., level nos. 36–39) are labeled in Figures 4–9. In each figure, the sum ( $I_l + I_r$ ) and difference ( $I_l - I_r$ ) emission intensity scales are expressed in identical, but otherwise arbitrarily chosen, intensity units.



**Figure 8.** Spectra obtained from circularly polarized, axial emission measurements in the  ${}^7F_2 \leftarrow {}^5D(3)_4$  transition region of  $Tb^{3+}(4f^8)$  in TbODA. Sample temperature was ca. 20 K, and sample excitation was with the 488 nm output of an argon ion laser. See text for an explanation of peak numbering.

The  $(I_l - I_r)$  spectra shown in Figures 4–9 are commonly referred to as *circularly polarized luminescence* (or CPL) spectra,<sup>2,39</sup> and they carry information about the *chirality-dependent* properties of optical emission processes in TbODA. These spectra are the emission analogues of circular dichroic absorption spectra (or CD spectra), which carry information about the chirality-dependent properties of optical absorption processes. The circular differential emission intensity quantities,  $\Delta I = I_l - I_r$ , and emission dissymmetry factors,  $g_{em} = 2\Delta I / (I_l + I_r)$ , measured in CPL spectroscopy are analogous to the circular differential absorptivity quantities,  $\Delta\epsilon = \epsilon_l - \epsilon_r$ , and absorption dissymmetry factors,  $g_{ab} = 2\Delta\epsilon / (\epsilon_l + \epsilon_r)$ , measured in CD spectroscopy. It has become common practice in both CD and CPL spectroscopy studies to use the dimensionless absorption and emission dissymmetry factors,  $g_{ab}$  and  $g_{em}$ , as measures of the *degree* and *sense* of chiroptical activity in individual absorption and emission lines (and their corresponding transitions). The magnitudes and signs of these quantities depend on the mechanistic details of the transitions under study, and they also depend on the degree and sense of structural chirality in the optically active absorbing or emitting species.

For most electronic transitions observed in the great majority of optically active (chiral) systems, the largest contributions to CD or CPL line strengths derive from interferences between electric and magnetic dipole transition amplitudes in the underlying optical processes.<sup>2,39</sup> The dissymmetry factors



**Figure 9.** Spectra obtained from circularly polarized, axial emission measurements in the  ${}^7F_{0,1} \leftarrow {}^5D(3)_4$  transition regions of  $Tb^{3+}(4f^8)$  in TbODA. Sample temperature was ca. 20 K, and sample excitation was with the 488 nm output of an argon ion laser. See text for an explanation of peak numbering.

observed in the CD/absorption and CPL/emission spectra of these transitions may be expressed as

$$g_{ab}(i) = \frac{4|\mathbf{P}_i||\mathbf{M}_i|\cos\theta_i}{|\mathbf{P}_i|^2 + |\mathbf{M}_i|^2} \quad (7)$$

$$g_{em}(j) = \frac{4|\mathbf{P}_j||\mathbf{M}_j|\cos\theta_j}{|\mathbf{P}_j|^2 + |\mathbf{M}_j|^2} \quad (8)$$

where  $i$  and  $j$  are transition labels;  $\mathbf{P}_{i(j)}$  and  $\mathbf{M}_{i(j)}$  denote, respectively, the electric and magnetic dipole transition vectors of the indicated absorptive (or emissive) transition; and  $\theta_{i(j)}$  is the angle between  $\mathbf{P}_{i(j)}$  and  $\mathbf{M}_{i(j)}$ . In our discussion here, it will be useful to reformulate eqs 7 and 8 to show the dependence of  $g_{ab}(i)$  and  $g_{em}(j)$  on the *ratios* of electric and magnetic dipole transition amplitudes:<sup>40</sup>

$$g_{ab}(i) = \frac{4(P_i/M_i)\cos\theta_i}{(P_i/M_i)^2 + 1} \quad (9)$$

$$g_{em}(j) = \frac{4(P_j/M_j)\cos\theta_j}{(P_j/M_j)^2 + 1} \quad (10)$$

where  $P_{i(j)}$  and  $M_{i(j)}$  represent the magnitudes (or lengths) of the transition vectors  $\mathbf{P}_{i(j)}$  and  $\mathbf{M}_{i(j)}$ . These expressions show

(38) Jayasankar, C. K.; Reid, M. F.; Richardson, F. S. *J. Less-Common Met.* **1989**, *148*, 289.

(39) Riehl, J. P.; Richardson, F. S. *Chem. Rev.* **1986**, *86*, 1.

(40) Metcalf, D. H.; Richardson, F. S. *J. Alloys Compd.* **1994**, *207/208*, 59.

that the values of  $g_{ab}(i)$  and  $g_{em}(j)$  will approach their upper and lower limits (+2 and -2) when  $\cos \theta_{i(j)} = \pm 1$  and  $(P_{i(j)}/M_{i(j)}) \rightarrow 1$ .

In axially symmetric optically active chromophores or luminophores, such as  $\text{Tb}(\text{oda})_3^{3-}$  complexes in TbODA, the  $\mathbf{P}_{i(j)}$  and  $\mathbf{M}_{i(j)}$  vectors of each dipole-allowed transition must be either parallel or antiparallel (i.e.,  $\theta_{i(j)} = 0$  or  $180^\circ$ ), and, therefore, the  $\cos \theta_{i(j)}$  functions for all of the CD and CPL active transitions are constrained to values of  $\pm 1$ . It follows that the magnitudes of the dissymmetry factors observed for these transitions are determined entirely by the  $P_{i(j)}/M_{i(j)}$  ratios shown in eqs 9 and 10. Most of the transitions observed in the CD/absorption and CPL/emission spectra of TbODA exhibit  $|g_{ab}|$  or  $|g_{em}|$  values that are  $< 0.3$ , which implies that the  $P_{i(j)}/M_{i(j)}$  ratios for most of these transitions are either  $> 13$  or  $< 0.08$ . The largest dissymmetry factors are observed in the  ${}^7\text{F}_{3,5} \leftarrow {}^5\text{D}(3)_4$  transition regions of the CPL/emission spectra (see Figures 5 and 7). Results obtained from our linearly ( $\sigma$  versus  $\pi$ ) polarized emission measurements show that many of the lines observed in these transition regions exhibit significant admixtures of electric *and* magnetic dipole character.

### Conclusion

Among all the LnODA systems examined to date, TbODA posed the most difficult challenges for crystal-field energy-level location, assignment, and analysis. The  $4f^8(\text{Tb}^{3+})$  electronic state structure in TbODA is relatively dense, and there is

extensive mixing and overlapping between and among many of the excited  $J$  multiplet manifolds. Location and assignment of crystal-field levels required use of the full complement of spectroscopic measurements performed in this study: unpolarized, linearly polarized, and circularly polarized optical absorption and emission measurements on single-crystal samples over a wide range of sample temperatures. The energy-level modeling calculations performed in this study produced reasonably good fits between calculated and experimentally observed energy-level structure in the  $4f^8[\text{SL}]J$  multiplet manifolds of  $\text{Tb}^{3+}$ , and they proved sufficient for characterizing the  $4f$  electron/crystal-field interaction strengths and anisotropies in TbODA. The overall crystal-field interaction strength ( $S_{cf}$ ) determined for TbODA was found to be ca. 45% greater than that determined for DyODA, and it is greater than those determined for all other members of the LnODA series. The degree of chiroptical activity observed in the CD/absorption and CPL/emission spectra of TbODA is somewhat greater than that observed for most optically active systems, but it is comparable to that observed in the analogous spectra of other LnODA systems. The relatively strong chiroptical activity exhibited by TbODA and the other LnODA systems reflects, in large part, the relatively strong admixtures of electric *and* magnetic dipole strength in the  $4f-4f$  transitions of these systems.

**Acknowledgment.** This work was supported by the U.S. National Science Foundation.

IC971114N